



Use of Radio Occultation Data in Ionospheric Assimilation Algorithm IDA4D

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ASTRA Overview

❖ Science
❖ Technology
❖ Applications
Bringing It All Together

Spaceweather
Modeling

Data
Assimilation

Data
Analysis

Instrument
Development

Space
Systems

TIMEGCM

AMIE
High-latitude
Electrodynamics

Space Based
Data

Ground
Based Data

HF TID Mapper

GPS-based Space
Weather Monitor

NSF DICE
CubeSat

SMC SENSE

IDA4D
Global
Ionosphere

Fabry-Perot
Interferometer

Plug-N-Play
Avionics

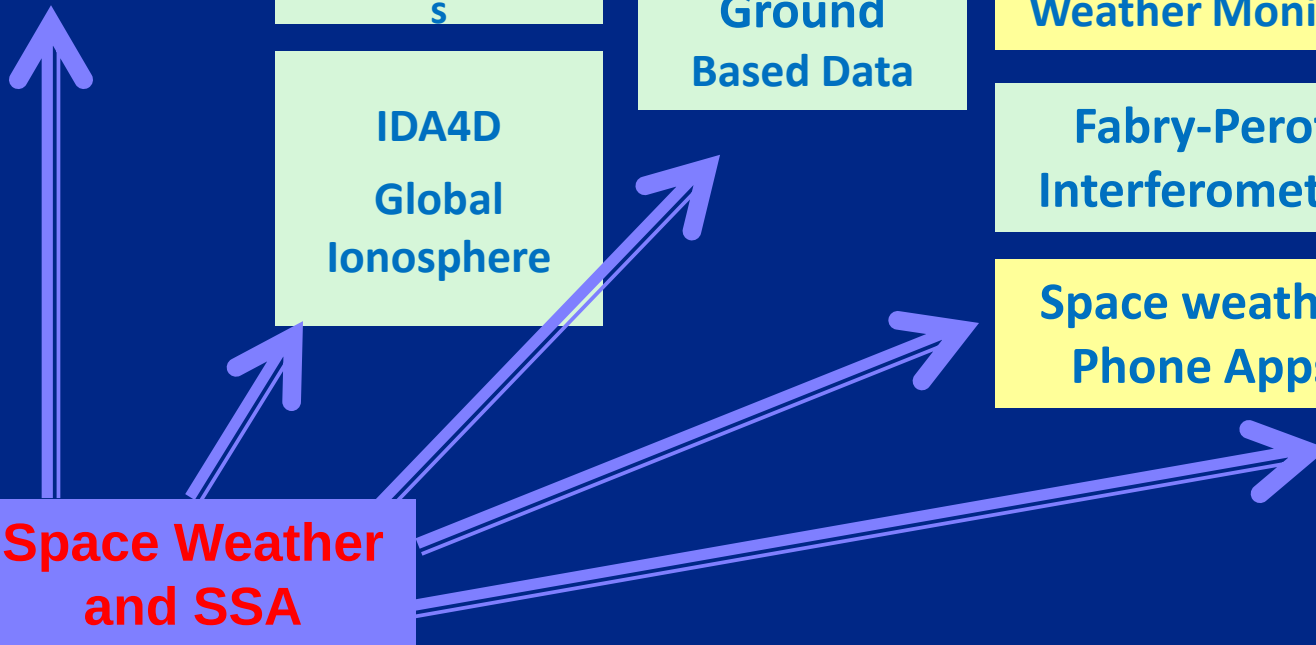
Scanning
Photometer
System

Space-based
GPS receiver

Temperature
Sensor (Balloon)
& Dosimeter

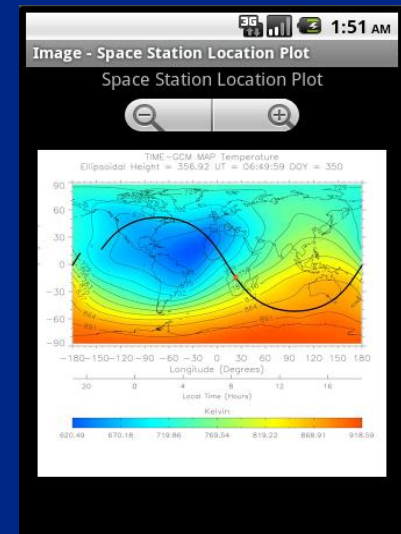
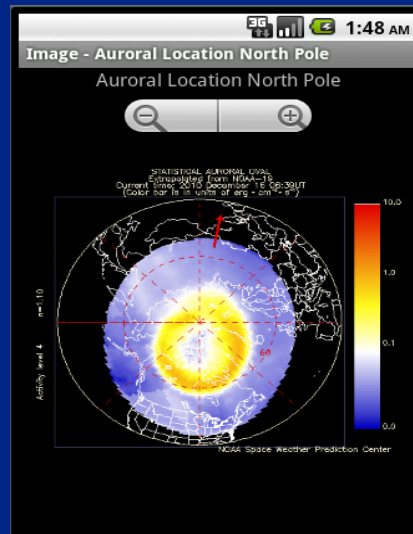
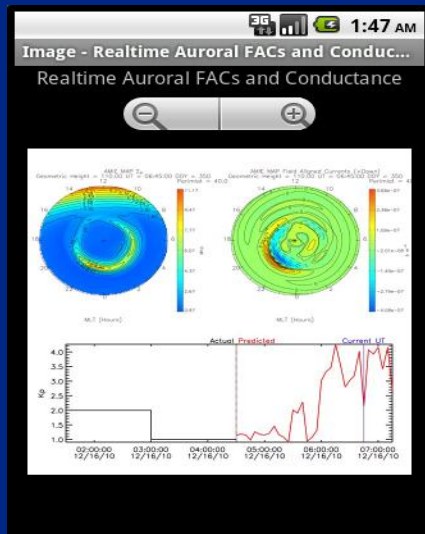
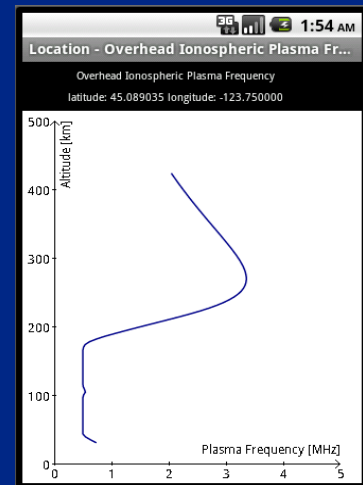
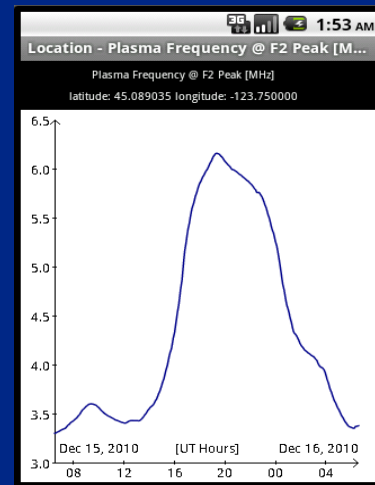
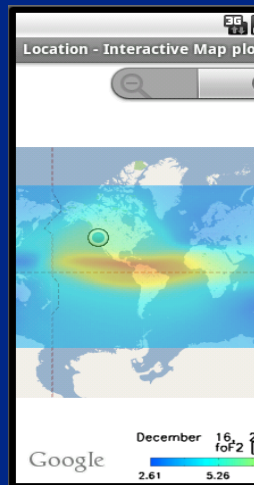
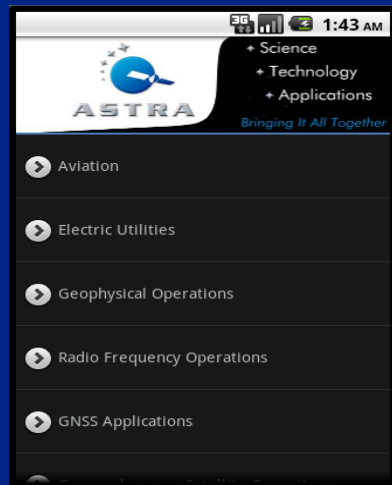
Space weather
Phone Apps

Space Weather
and SSA





REALTIME SPACE-WEATHER: ASTRA Space Weather App



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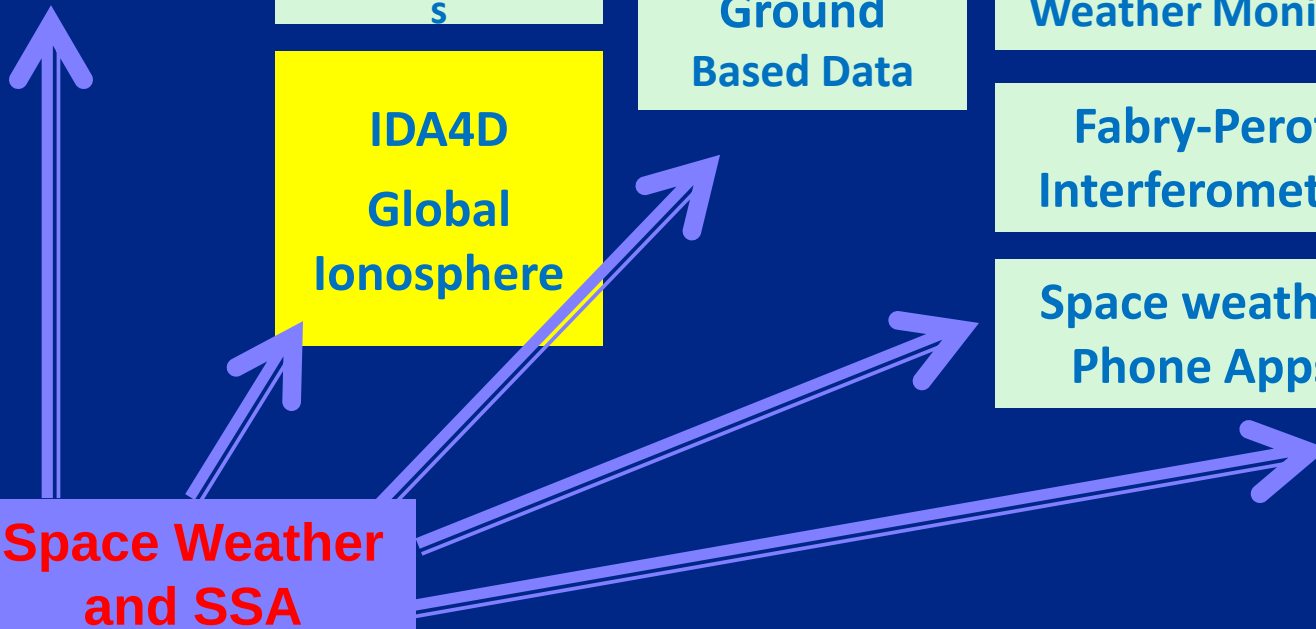
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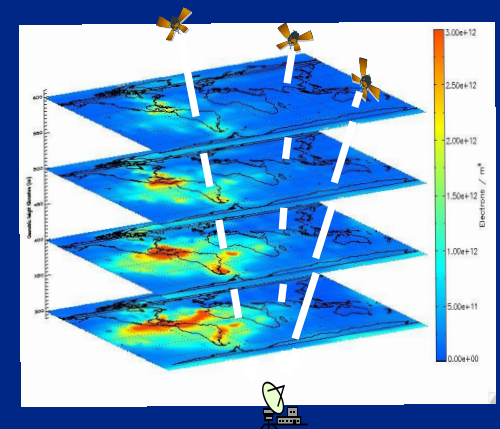
IDA4D
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Outline

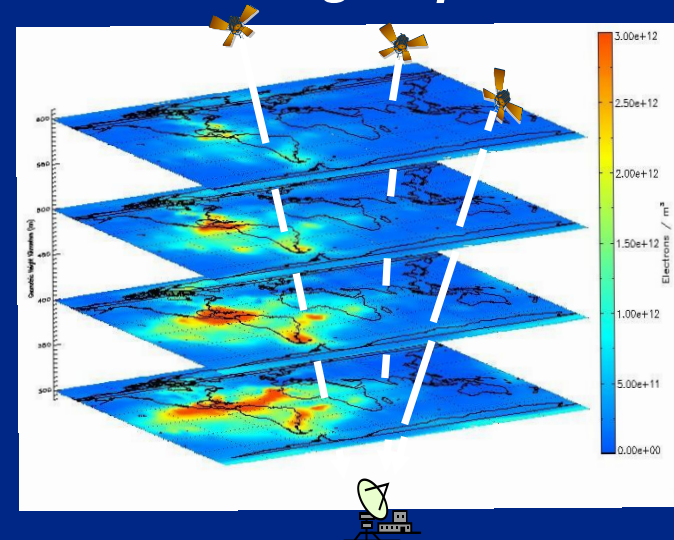
- **Description of IDA4D**
 - History of Radio Occultations in IDA4D
 - Example results
- **Using IDA4D to improve E-region density retrievals**
 - Method
 - Low-latitude climatology
 - High-latitude conductances
- **Simulation: GEOScan 66 Satellite Radio Occultation**
- **Simulation: CubeSat RO vs UV**
- **Summary**





Ionospheric Data Assimilation Four Dimensional IDA4D

- **Global 3D time-evolving imaging of the ionosphere electron density**
 - Gauss Markov Kalman Filter predicts forward in time
- ***Solves for log of electron density***
 - *Guarantees positivity*
 - *Errors are more log normal distribution*
- ***Completely irregular horizontal grid, vector of vertical grid points***
 - User selectable
 - High resolution where desired
 - Can be dynamically chosen based on data
- **Configuration files**
 - *User configurable error covariance*
 - model of background ionosphere
 - Amount of and type of data
 - Regional/global
 - Time steps
 - Convergence criteria
 - Data sampling rates, averaging windows, sampling windows, data representation errors





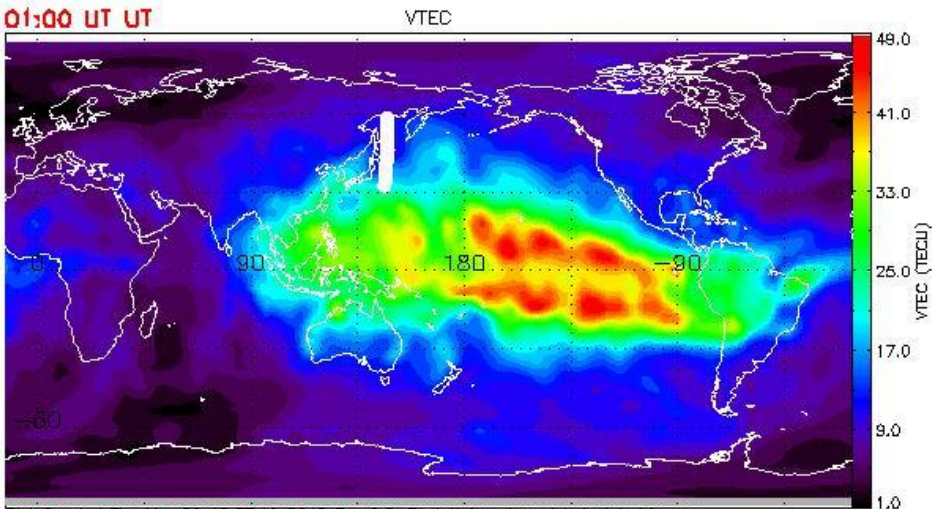
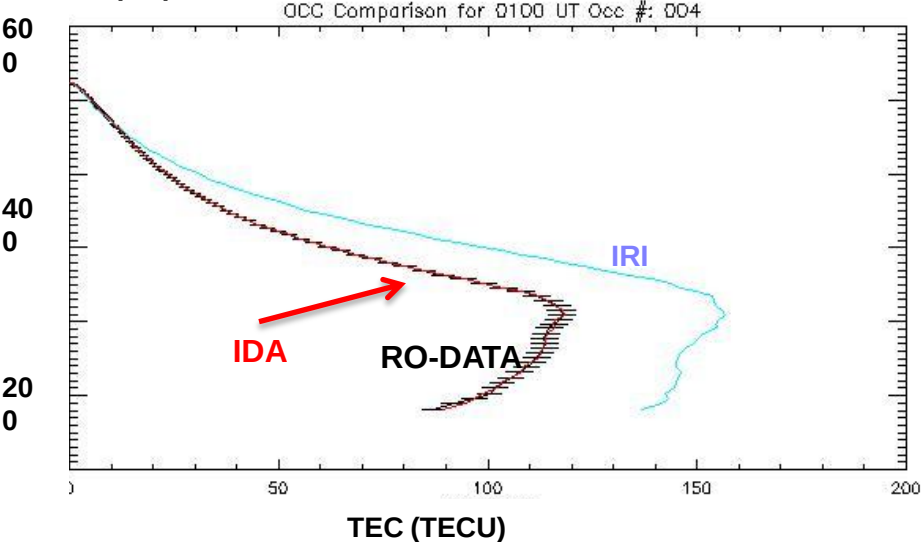
IDA4D and Radio Occultations

- IDA4D has routinely ingested slant TEC from Radio Occultations since 2002.
 - Slant TEC between LEO receiver and GPS transmitter
 - *not Abel inverted Ne profiles*
- IDA4D has ingested RO TEC from:
 - PICOSat, IOX, CHAMP, SAC-C, GRACE and COSMIC
- Typical case with CHAMP, GRACE and 6 COSMIC:
April 1, 2007
 - 15 minute cadence for IDA4D analyses
 - 5 second averaging on occultation TEC
 - ~ 4000-5000 RO-TEC observations per 15 minute analysis

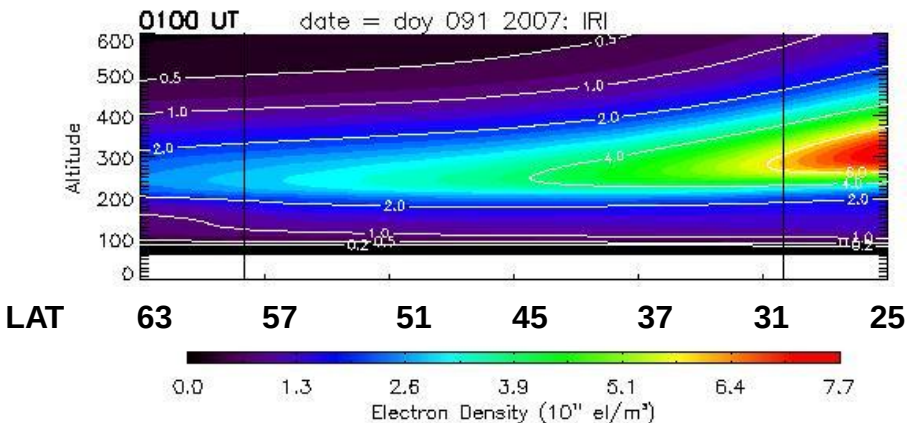
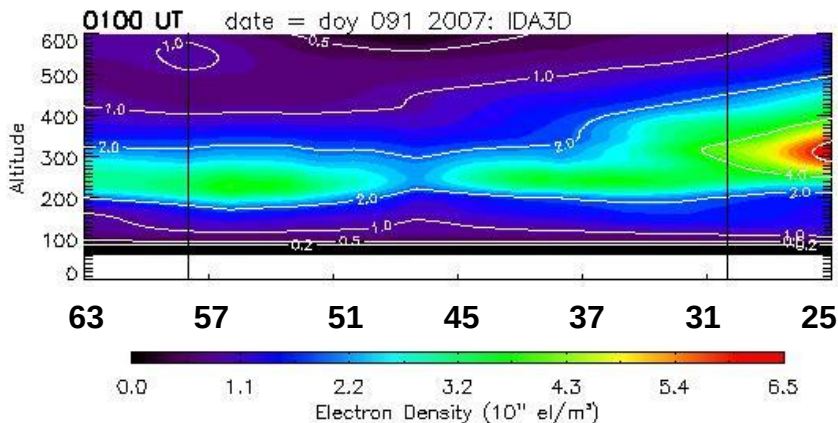


Example RO for 1 UT on April 1, 2007

Altitude (km)



0



E-region Densities from RO

The radio occultation technique

Now, if the distribution of electron density (n_e) in the ionosphere were spherically symmetric, at least over the region we are interested, we could write:

$$n_e(\text{lat}, \text{lon}, h) = n_e(r)$$

And we can show that $\text{TEC}(h_t)$ would be given by the so-called **Abel transform**:

$$\text{TEC}(h_t) = 2 \int_{h_t}^{\infty} \frac{n_e(r) r dr}{\sqrt{r^2 - h_t^2}}$$

Given TEC measurements, one can obtain $n_e(r)$ using the **inverse Abel transform**:

$$n_e(r) = -\frac{1}{\pi} \int_r^{\infty} \frac{d}{dh_t} \text{TEC}(h_t) \frac{dh_t}{\sqrt{h_t^2 - r^2}}$$

Unfortunately (or fortunately for some of us), **$n_e(\text{lat}, \text{lon}, h) = n_e(r)$ does not hold in most cases**, and horizontal density gradients should be taken into account when trying to obtain estimates of $n_e(h)$ from RO TEC observations.

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$$TEC(h_t) = 2 \int_{h_t}^{150} \frac{n_e(r) r dr}{\sqrt{r^2 - h_t^2}} + \int_{s_1}^{\infty} n_e(s_1) ds_1 + \int_{s_2}^{\infty} n_e(s_2) ds_2$$

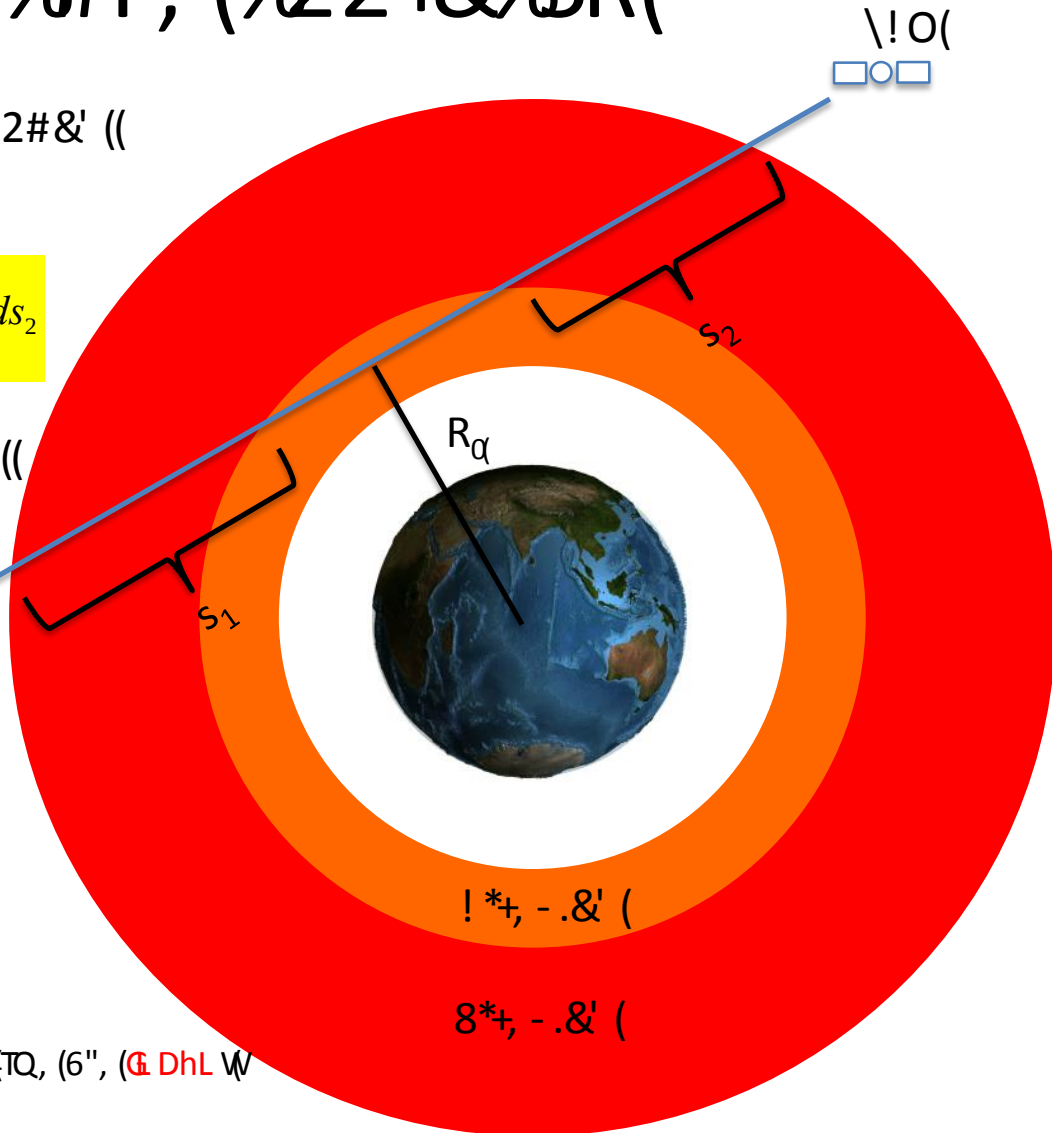
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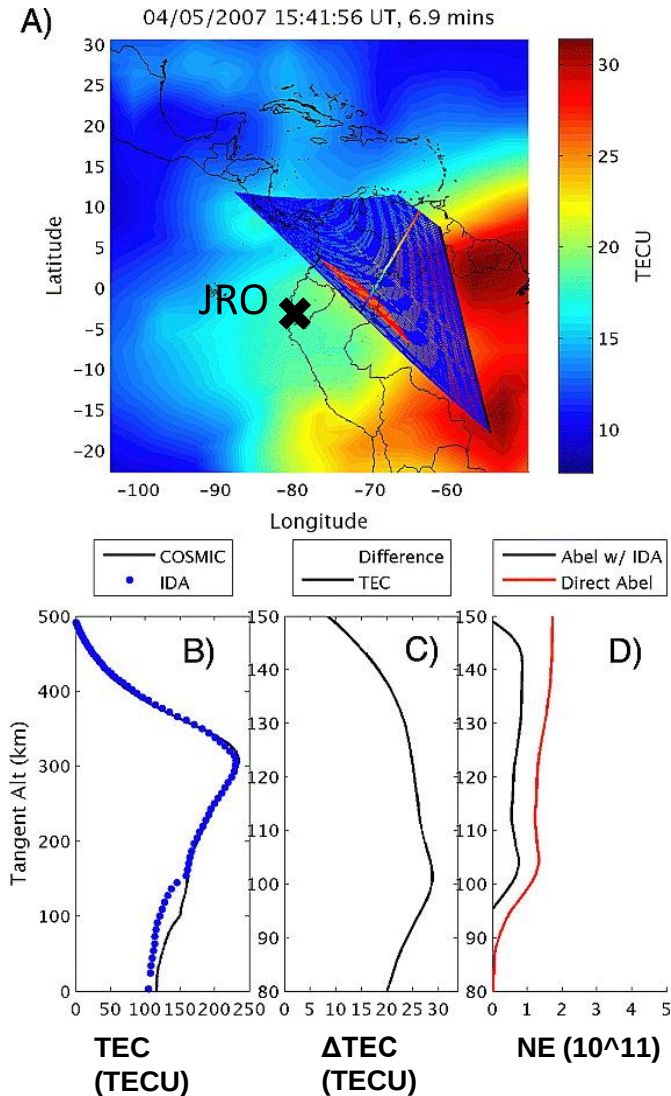
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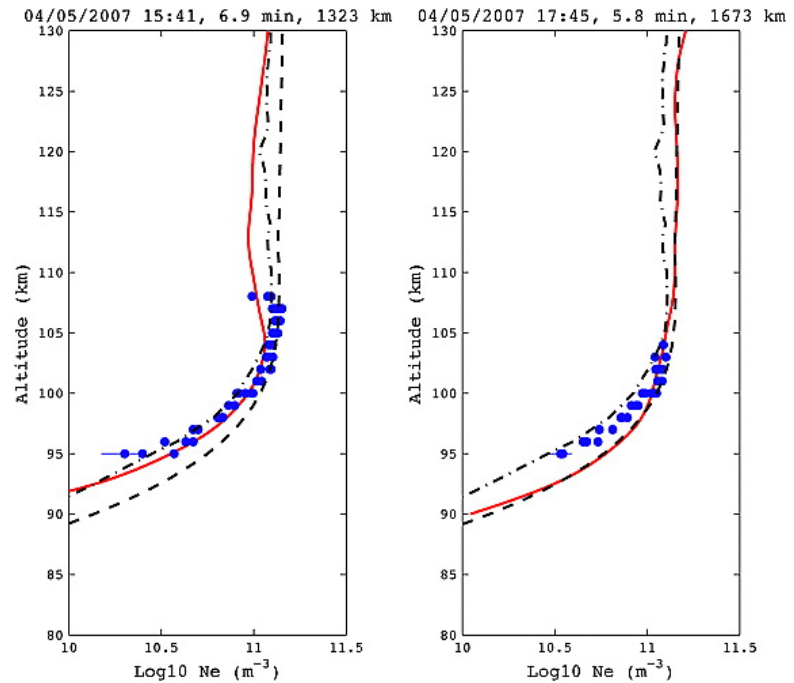
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Validation versus Radar Measurements



Validation/Comparison Analysis

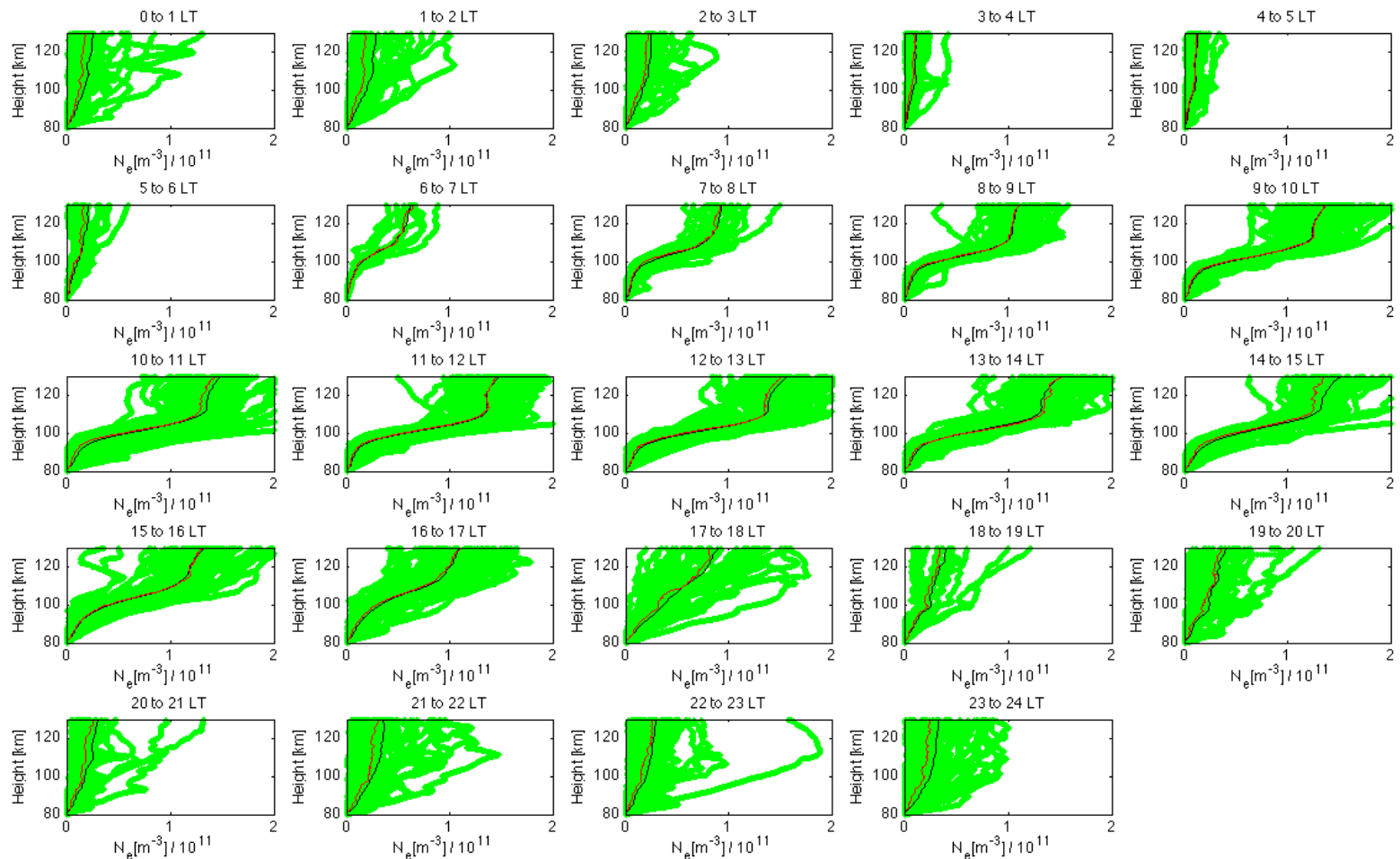


Jicamarca-Paracas Bistatic Radar
 - Inversion
 -.- FIRI
 -- IRI

Nicolls et al. (2009)

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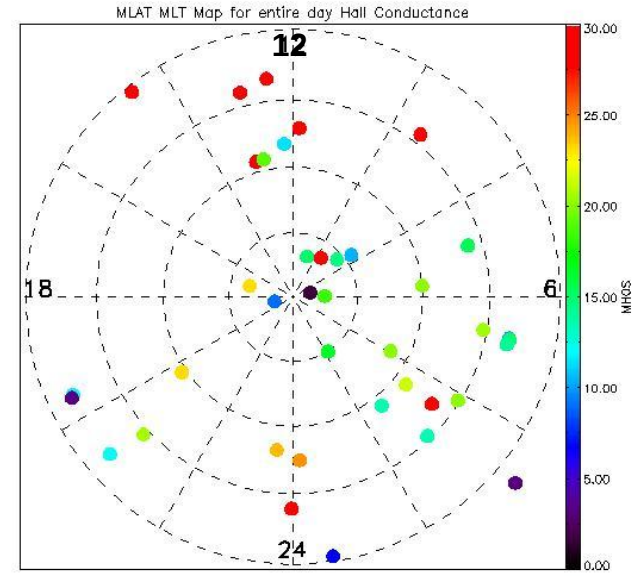
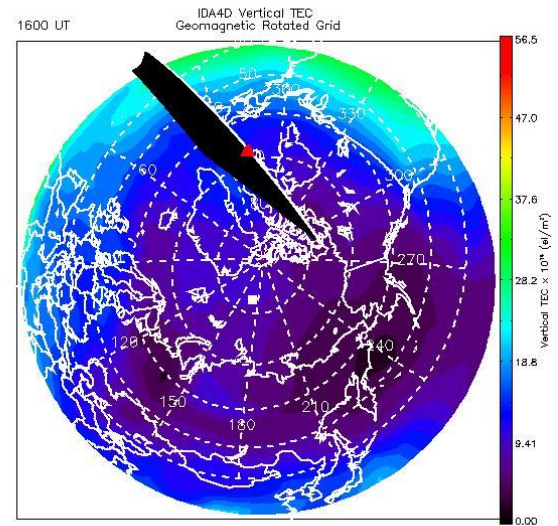
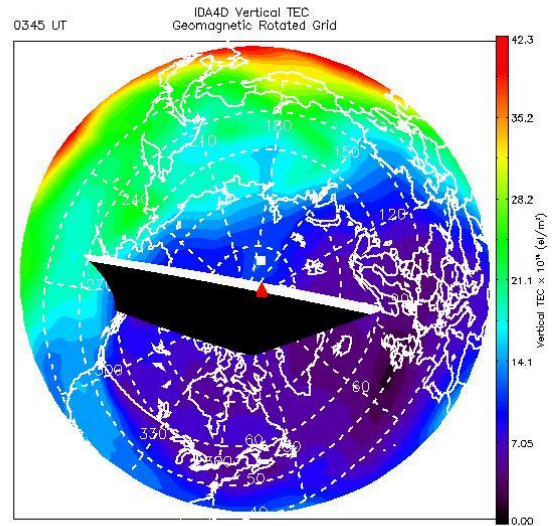
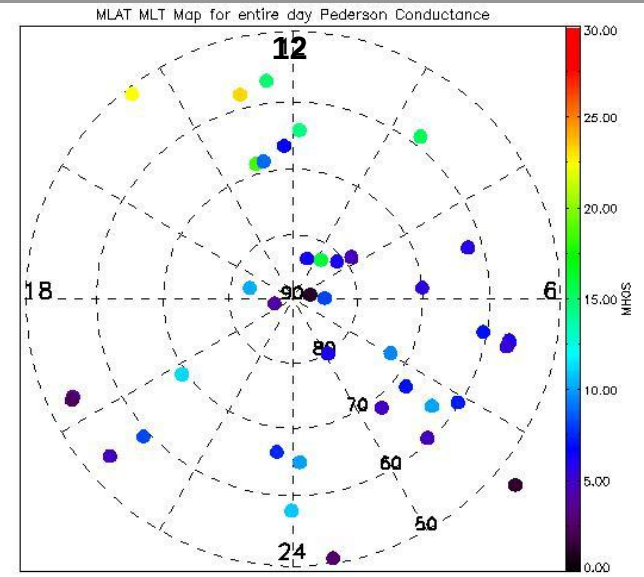
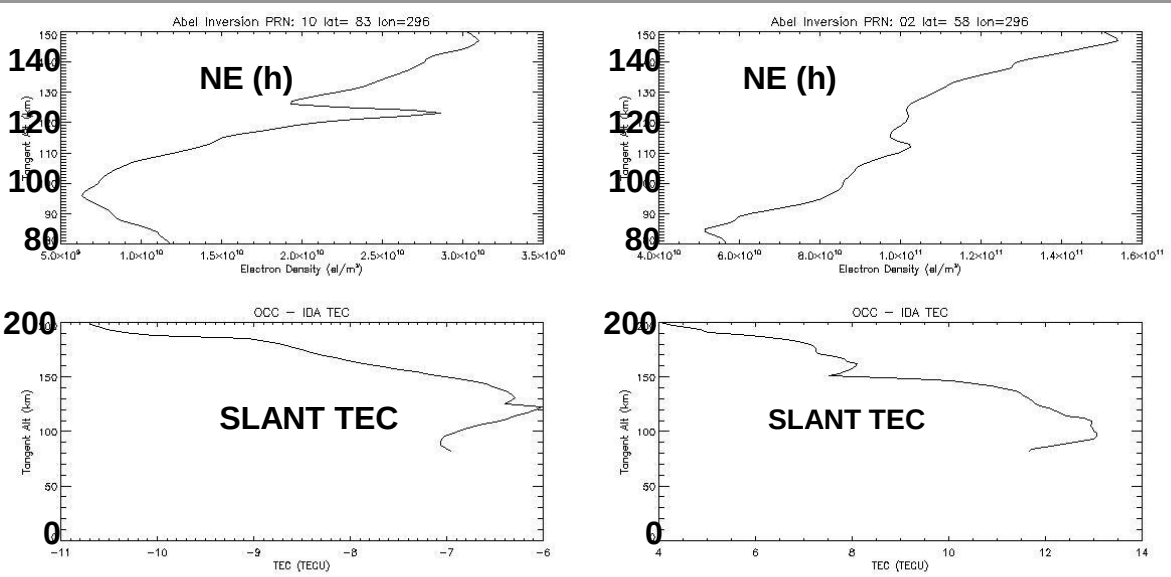
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Polar E-region Densities and Conductances



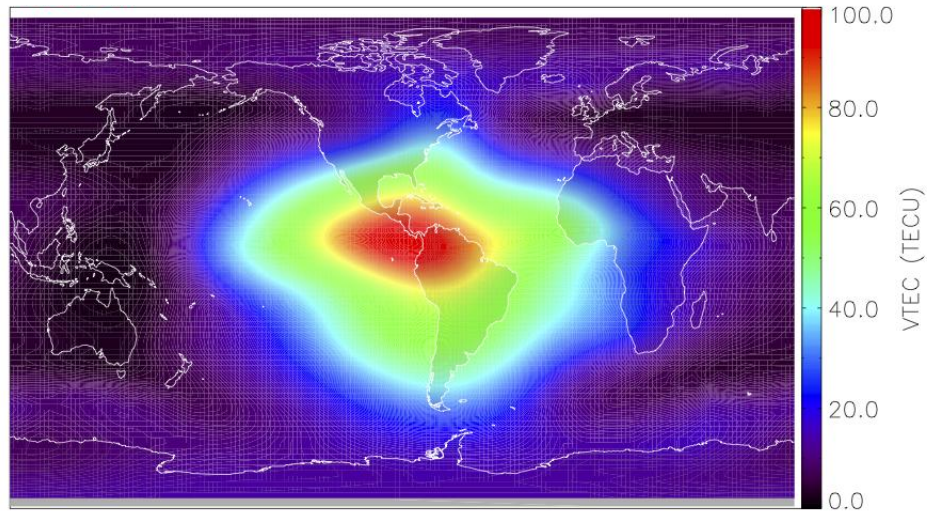


GEOScan: Simulating 66 LEO satellites with RO

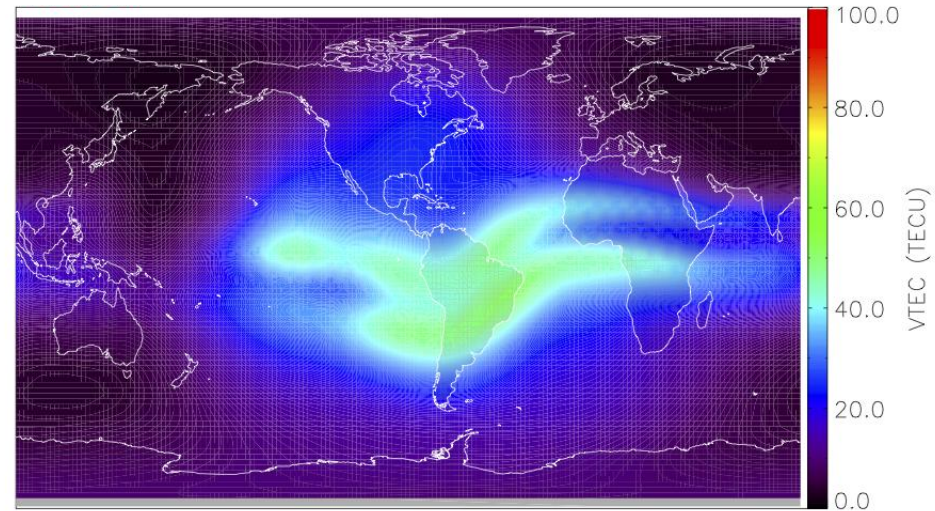
- 66 Iridium Satellites in Polar orbit at ~ 780 km altitude
- Simulate RO TEC data for 3 hours
 - November 20, 2003 Superstorm 15-18 UT
 - Use TIMEGCM simulation as “Ground Truth”
 - Fly all 66 satellites in actual Iridium orbital planes with correct geometry
 - Use actual GPS ephemeris for the day to get links between LEO Iridium receivers and GPS transmitters
 - Compute TEC using TIMEGCM “Truth”
- IDA4D Inversions
 - Use IRI as background model: *No mixing of “truth ionosphere” and background model in IDA*
 - Use ONLY RO TEC data. No ground GPS or any other kind of simulated data
 - Run for 3 hours, 5 minute cadences for IDA4D inversions
 - Do another run using only the actual ground GPS available for that day as a comparison

GEOScan Simulations

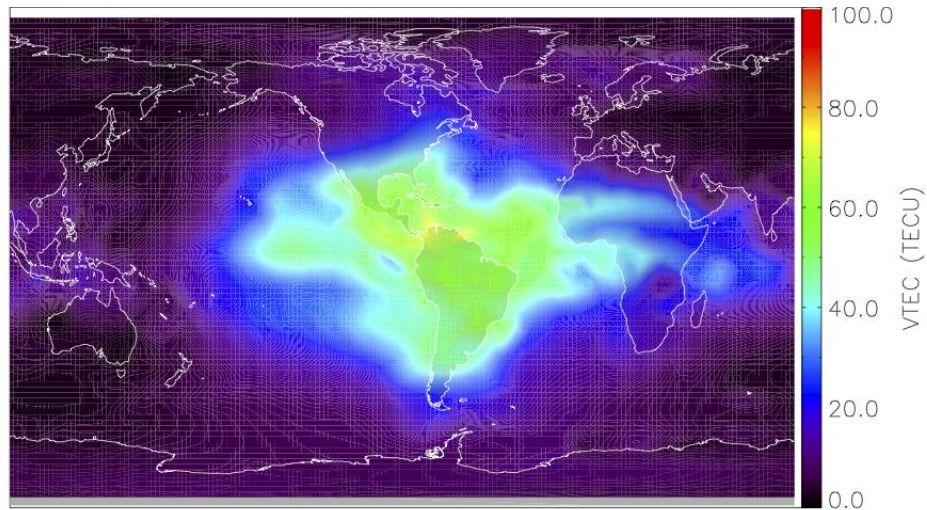
TRUTH



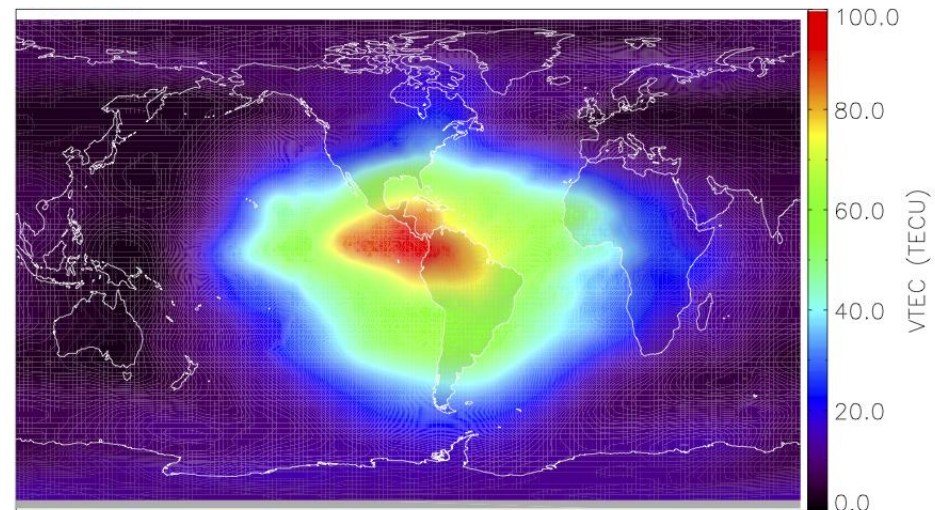
IRI



Ground-based GPS TEC



IDA4D



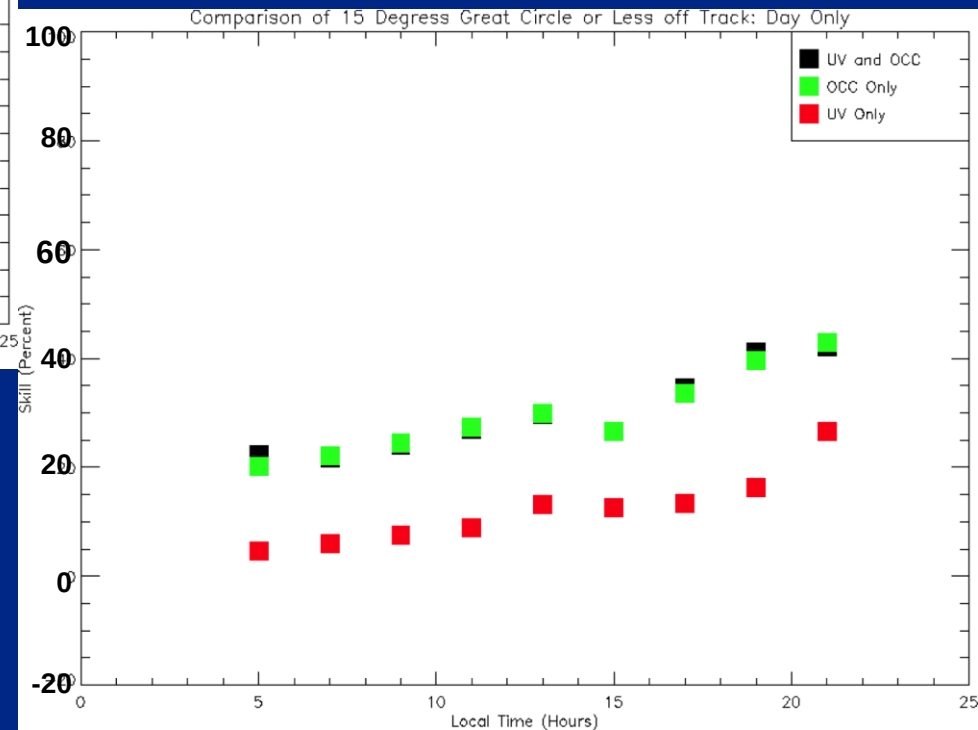
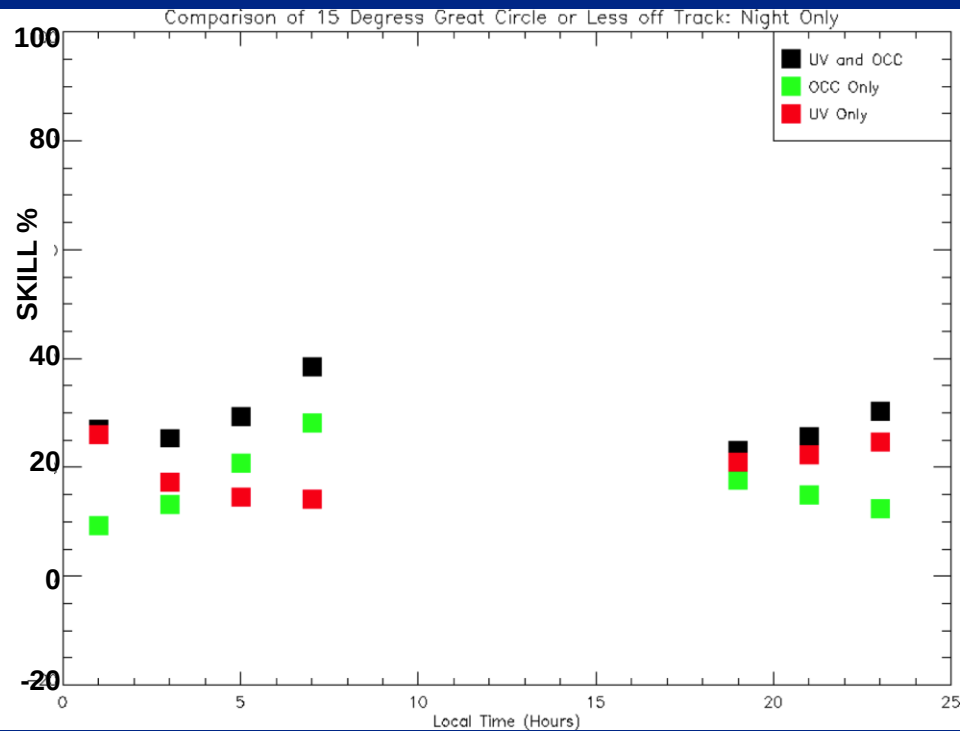


CubeSat Mission Simulations

- We performed simulations for 1 and 2 satellites in various orbital inclinations and altitudes.
- We simulated various scenarios with 1-2 instruments on each satellite – 650 km
- We quantified the performance against the simulated truth (again our old friend TIMEGCM November 20, 2003), and compared against ground GPS only as our baseline
- **Scenarios**
 - Ground GPS only
 - Ground GPS, Insitu electron density, Occultations
 - Ground GPS, Insitu electron density, Nadir 1356 Radiances (night only)
 - Ground GPS, Insitu electron density, Nadir 1356 Radiances (night only), Occultations
- **Skill score used to quantify performance**
 - **Baseline is the ground GPS-only case.**

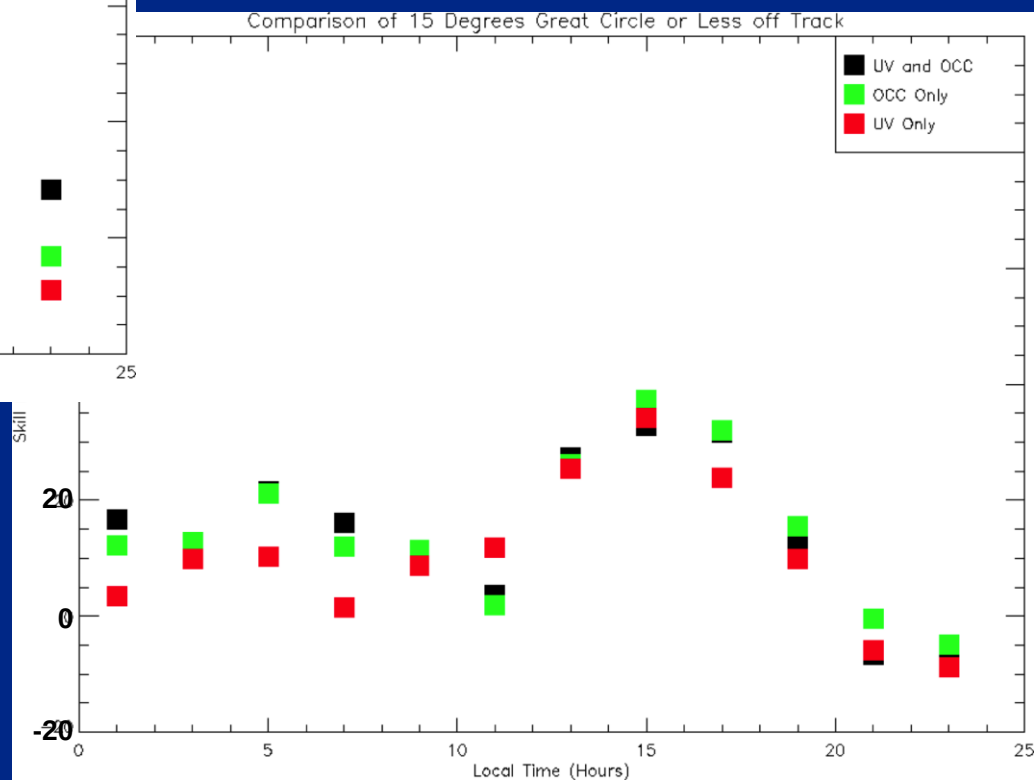
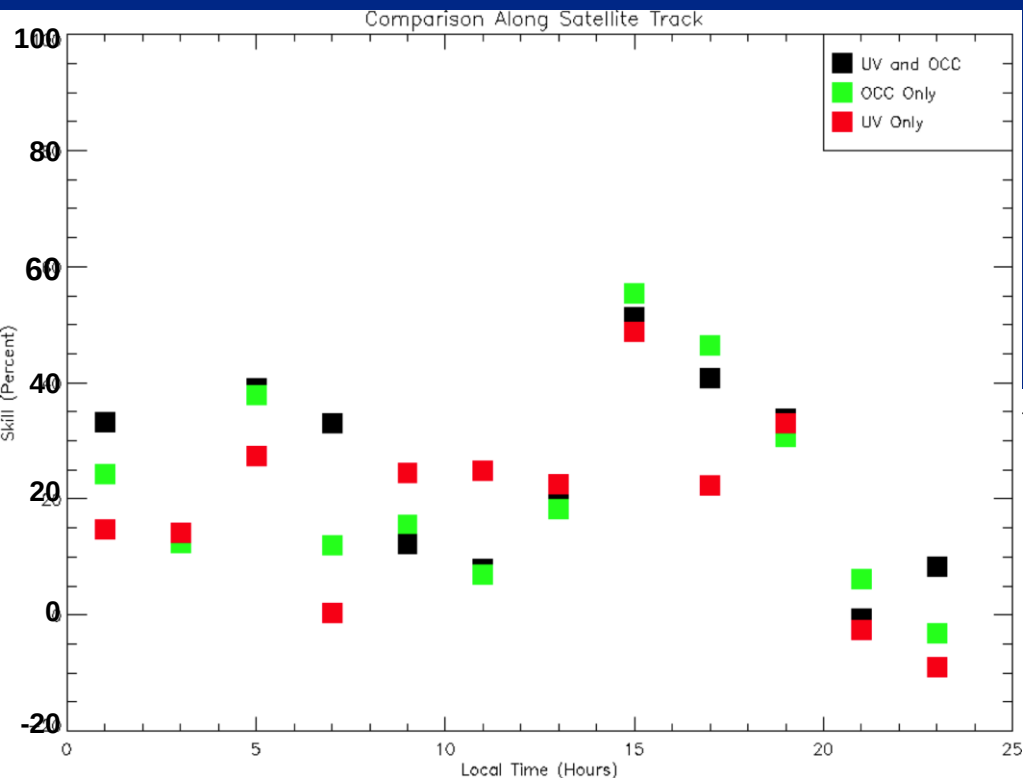


CubeSat Simulations: Skill Score for VTEC Retrievals





CubeSat Simulations: Skill Score for VTEC Retrievals





Summary

- IDA4D has routinely ingested RO TEC for ~10 years.
- IDA4D results have been used for science studies, applications, and simulations.
- A novel approach of combining IDA4D with RO TEC leads to improved estimates of E-region densities
- These E-region densities have been used to investigate low latitude climatology as well as high latitude conductances
- A 66 satellite GEOScan simulation of only RO TEC shows that such a dense satellite data set can completely (nearly) recover the original electron density.
 - needs more work, varying number of satellites
 - Seems capable of retrieving entire ionos, including horiz struc.
- Other simulations for Cubesats have shown the performance improvements obtained by RO.



Derivation of Skill Score Metric

D_i - IDA4D data point value

M_i - Baseline data point value

T_i, ν_i^T - Truth data point value, Truth variance

$$\psi_D^2 = \sum_i \frac{(D_i - T_i)^2}{\nu_i^T}$$

$$\psi_M^2 = \sum_i \frac{(M_i - T_i)^2}{\nu_i^T}$$

$$S = 1.0 - \sqrt{\frac{\psi_D^2}{\psi_M^2}}$$