

# GENERATION OF REFRACTIVITY CLIMATOLOGIES WITHOUT STATISTICAL OPTIMIZATION

Hans Gleisner (DMI), Sean Healy (ECMWF)

# Outline

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- *Bending angle to refractivity* processing
- Monthly mean bending angles in latitude bands
- Upper-level handling of the mean bending angles
- Non-linearities in the *BA* to *REF* processing
- Conclusions

# *BA* to *REF* processing

– single profiles –

- 1) Raw LC *BA* profiles  $\Rightarrow \alpha_{LC}(a)$
- 2) Statistical optimization  $\Rightarrow \alpha_{SO}(a)$
- 3) Inverse Abel transform  $\Rightarrow N(a)$
- 4) Change of height scale  $\Rightarrow N(H)$
- 5) Interpolation to common grid  $\Rightarrow N(H)$
- 6) Averaging in grid boxes  $\Rightarrow \langle N(H) \rangle$

Statistical optimization is foremost required for single-profile processing.

In the *ROtrends* study, statistical optimization was identified as a source of structural uncertainty [Steiner et al., 2012].

# BA to REF processing

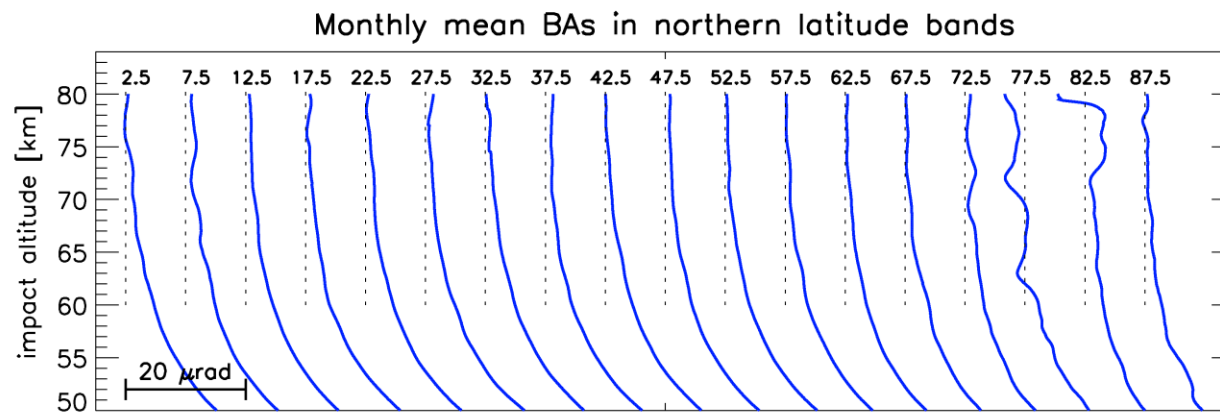
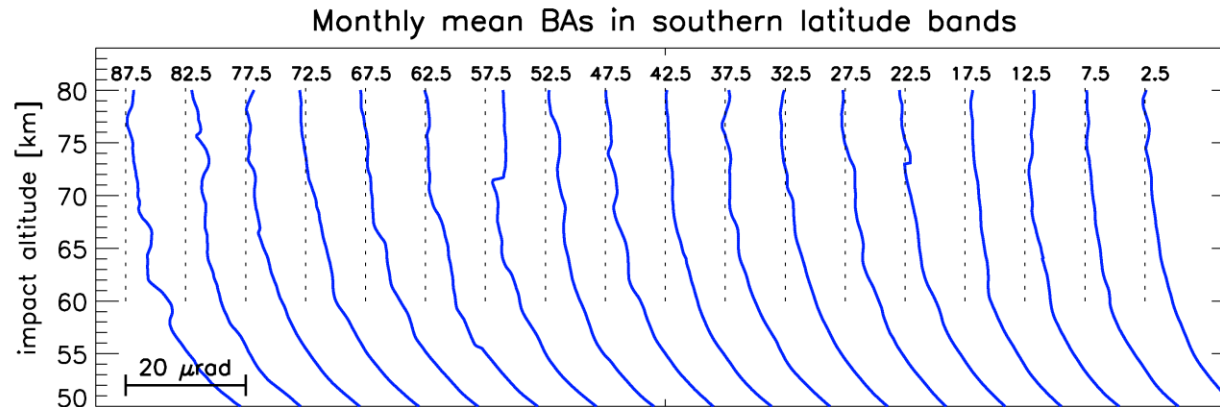
– zonal monthly means –

- |                                 |  |
|---------------------------------|--|
| 1) Zonal monthly mean grid      | $\Rightarrow \langle \alpha_{LC}(H_a) \rangle$ |
| 2) Upper level handling         | $\Rightarrow \langle \alpha_{LC}(H_a) \rangle$ |
| 3) Change of height scale       | $\Rightarrow \langle \alpha_{LC}(a) \rangle$   |
| 4) Inverse Abel transform       | $\Rightarrow \langle N(a) \rangle$             |
| 5) Change of height scale       | $\Rightarrow \langle N(H) \rangle$             |
| 6) Interpolation to common grid | $\Rightarrow \langle N(H) \rangle$             |

By processing a mean field instead of single profiles, we can use *observed* data up to higher altitudes, and thus reduce biases due to upper-level handling of the bending angles.

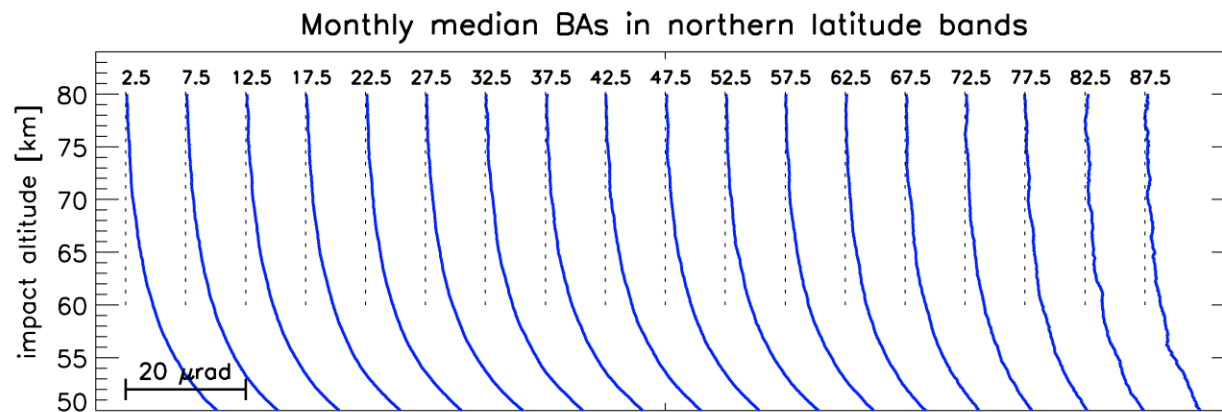
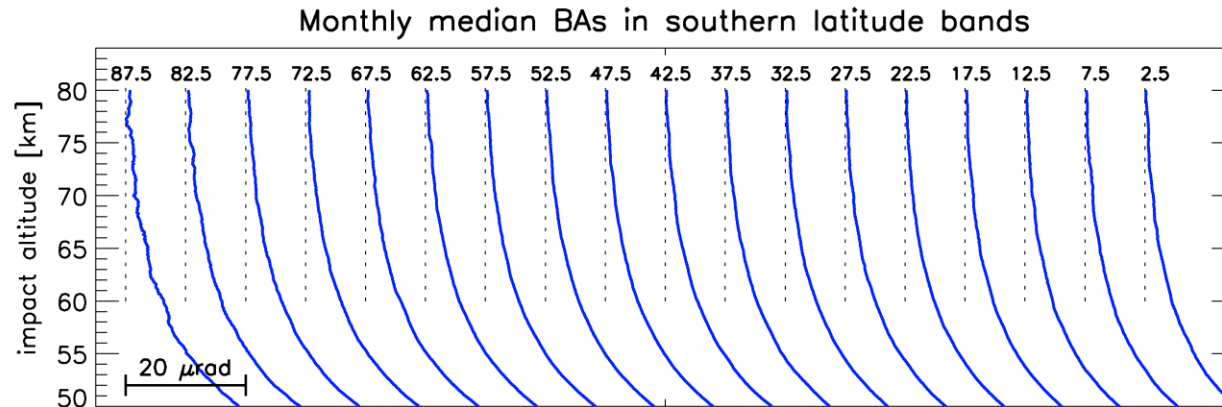
# Monthly mean bending angles

– means, COSMIC, Jan 2011 –



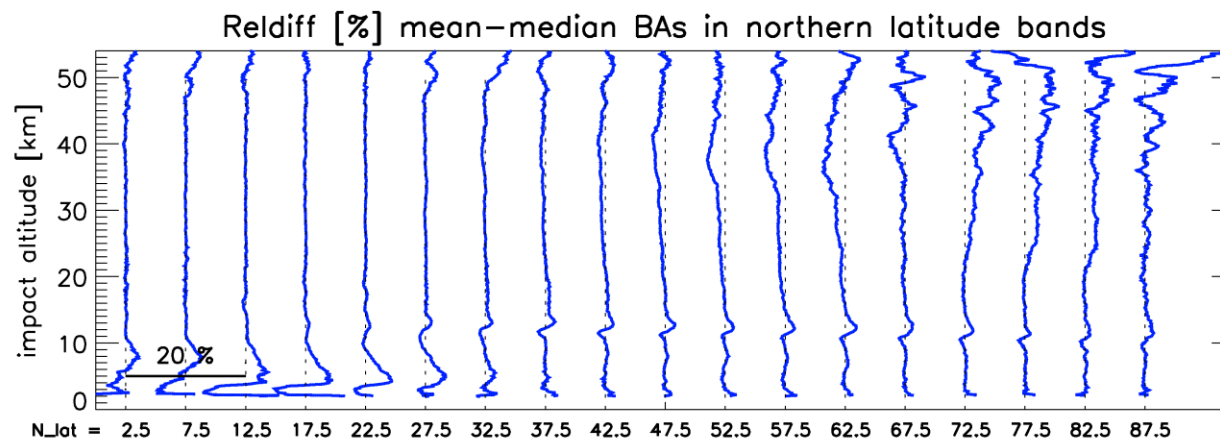
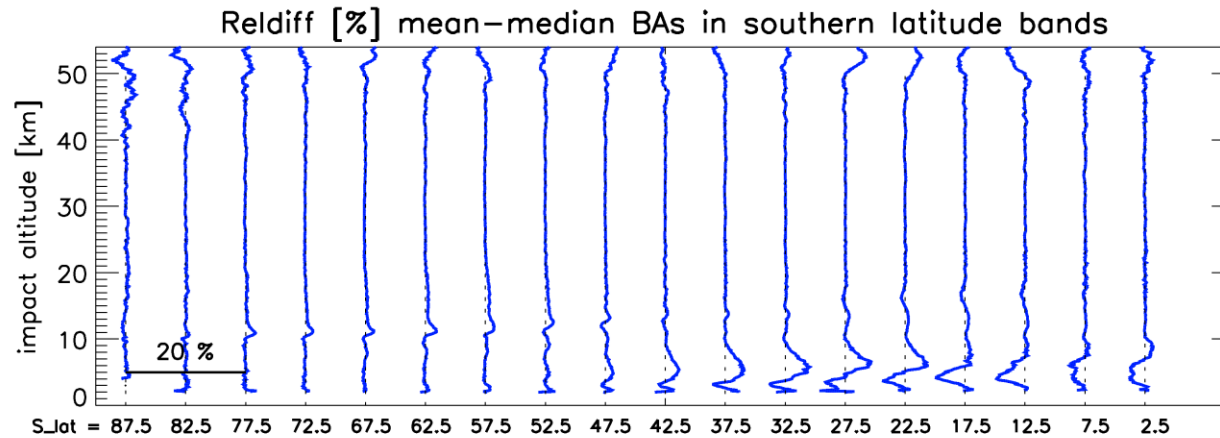
# Monthly mean bending angles

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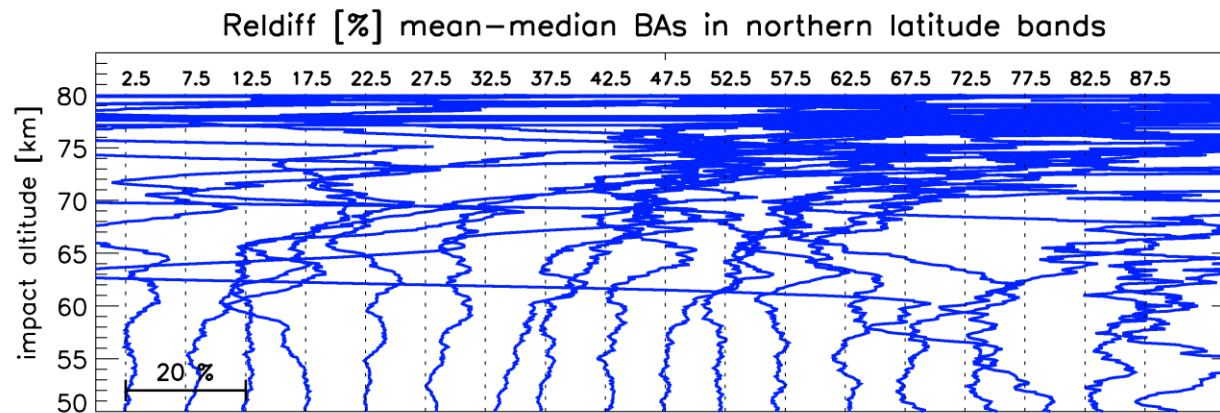
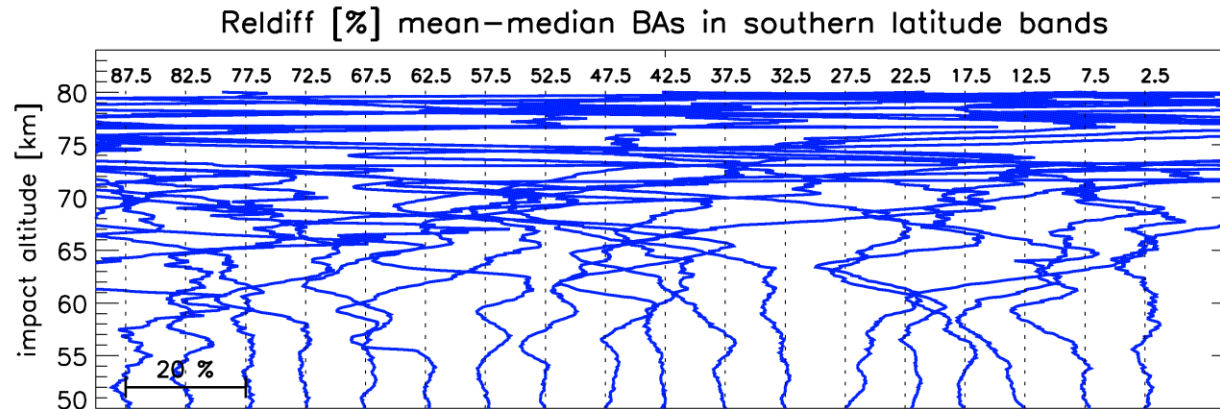
# Monthly mean bending angles

– reldiff mean-median, COSMIC, Jan 2011 –



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– reldiff mean-median, COSMIC, Jan 2011 –





# *BA to REF* processing

– zonal monthly means –

## **Steps 1 & 2: upper-level handling of mean bending angles**

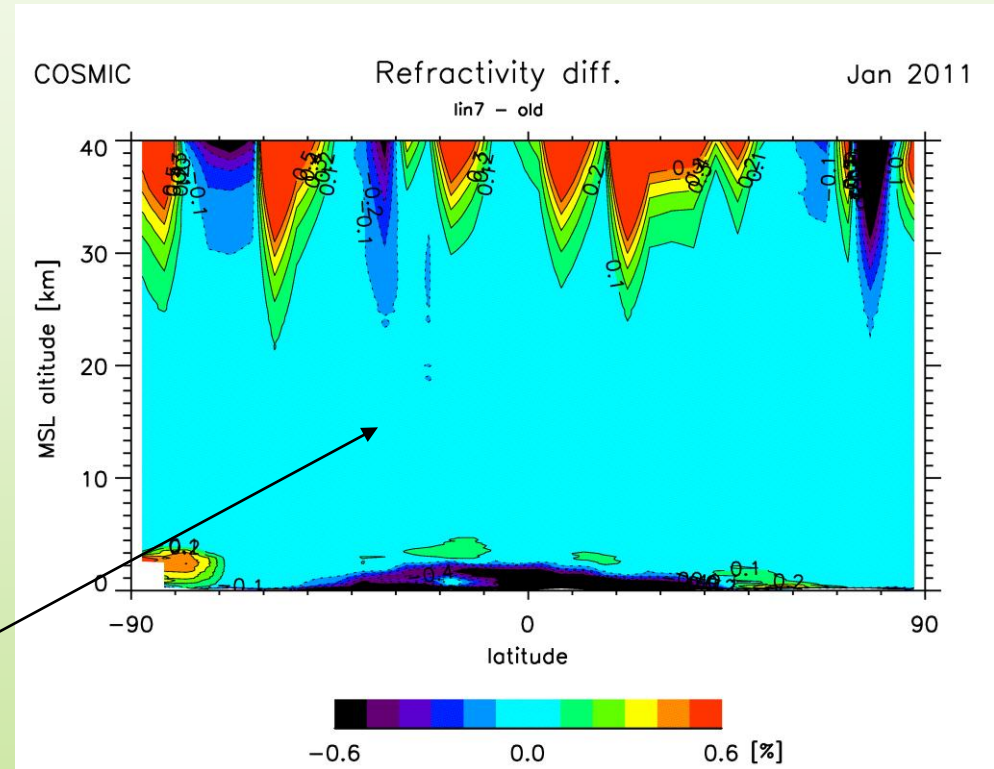
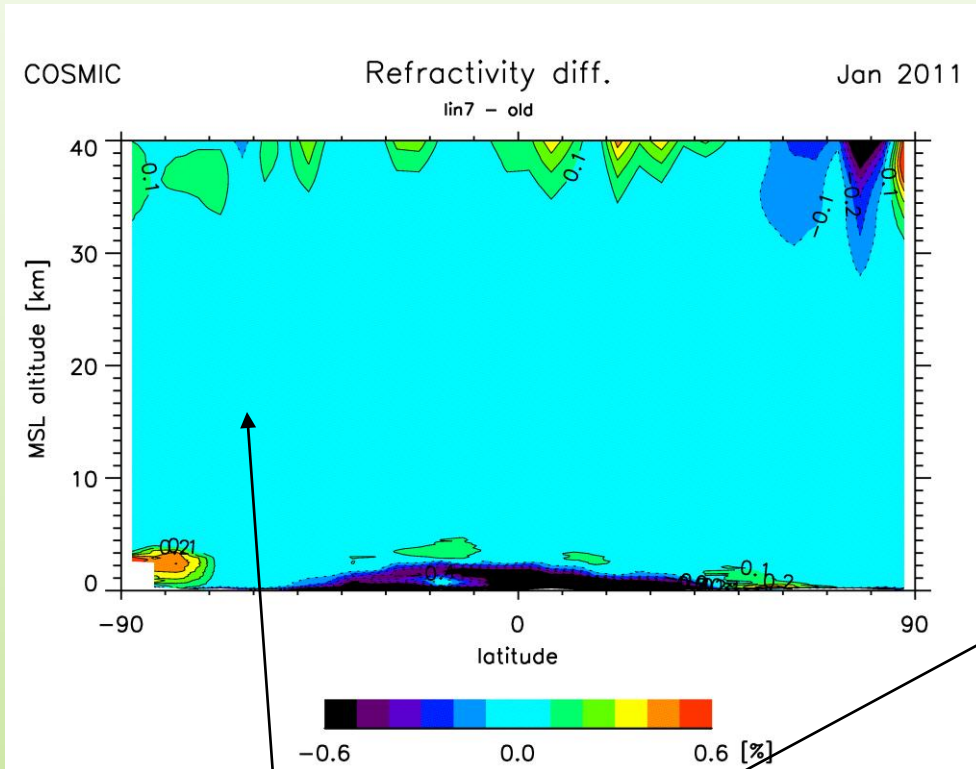
The zonal mean bending angles become increasingly noisy with altitude. Above 60 kilometers the *median*, rather than the *mean*, may provide a better description of the neutral-atmosphere bending angle.

We use:

- means up to 60 kilometers
- medians between 60 and 80 kilometers
- exponential fall-off above 80 kilometers

# Impact of median vs. mean

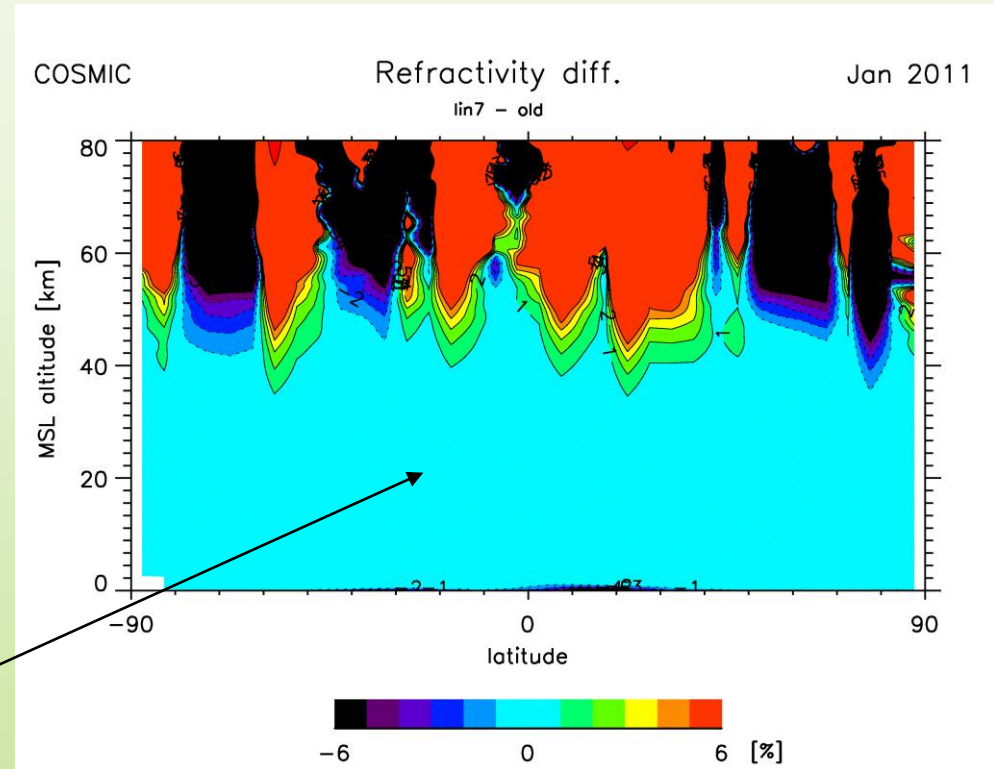
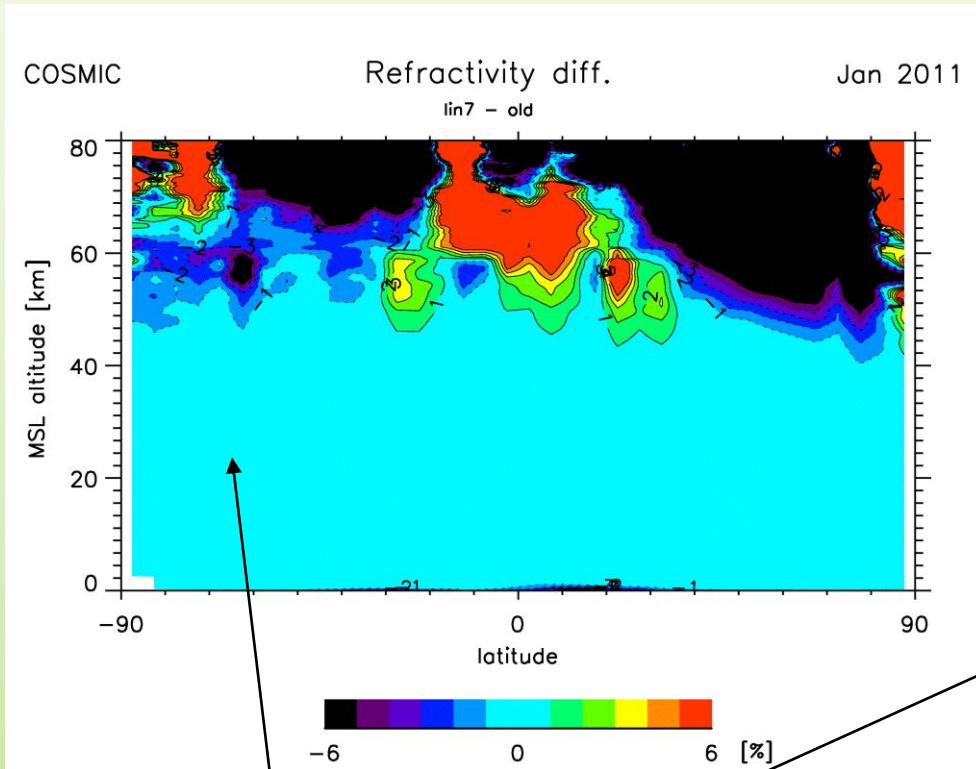
- agreement with single-profile processing –



The use of *median* instead of *mean* in the 60-80 km height range gives better agreement with climatologies from single-profile processing.

# Impact of median vs. mean

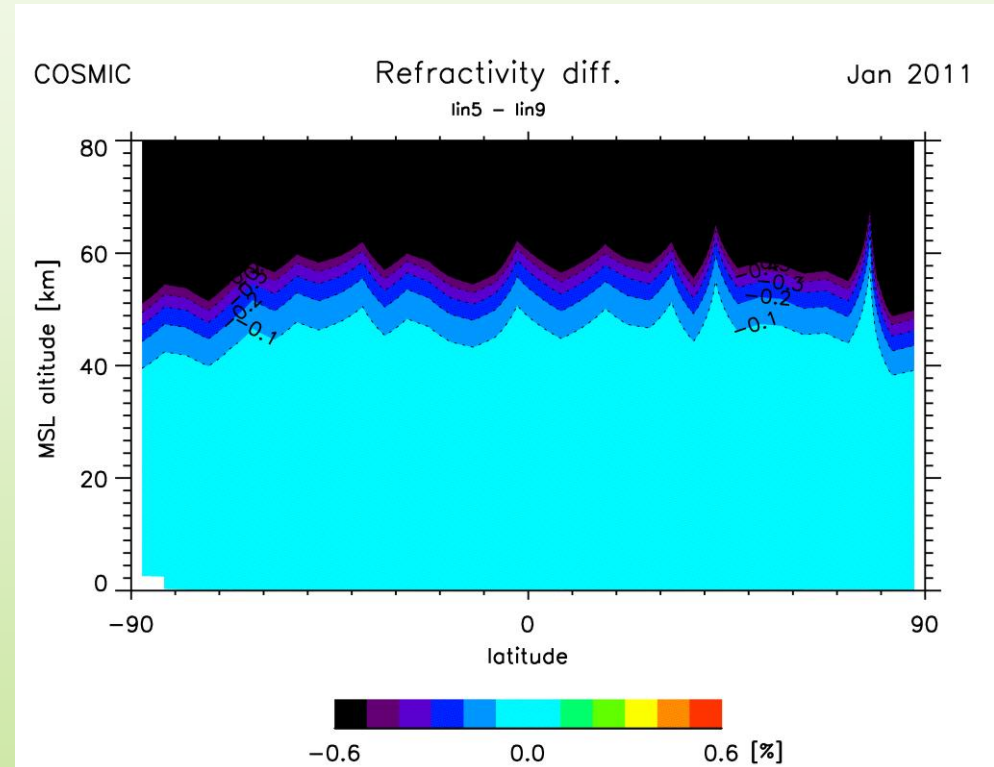
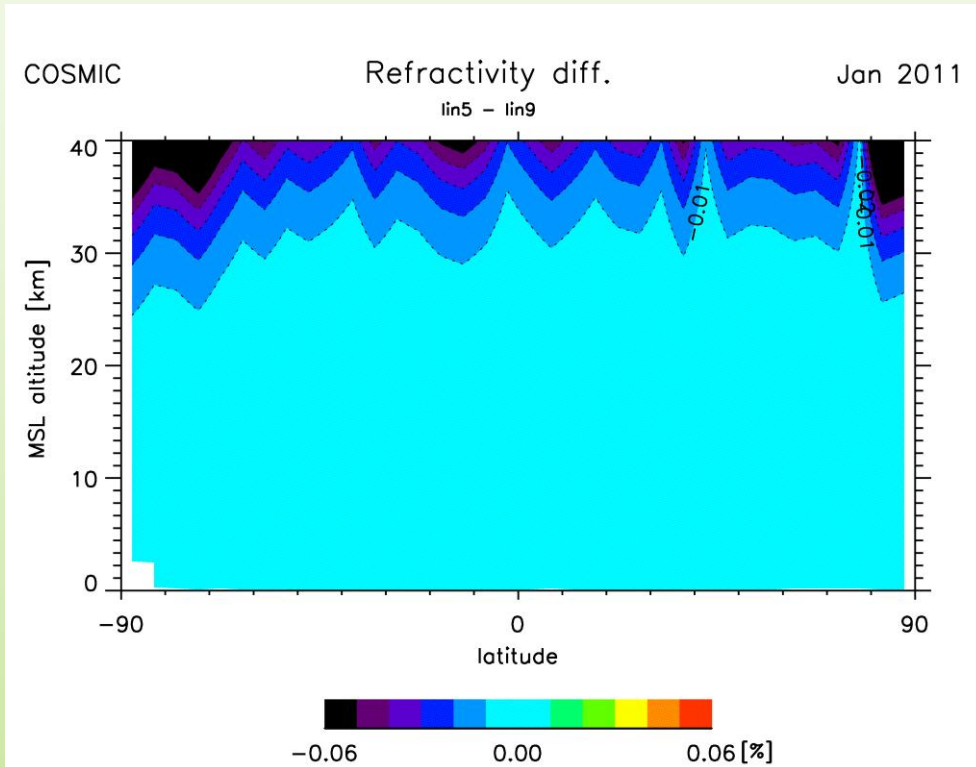
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# Impact of exponential extrapolation

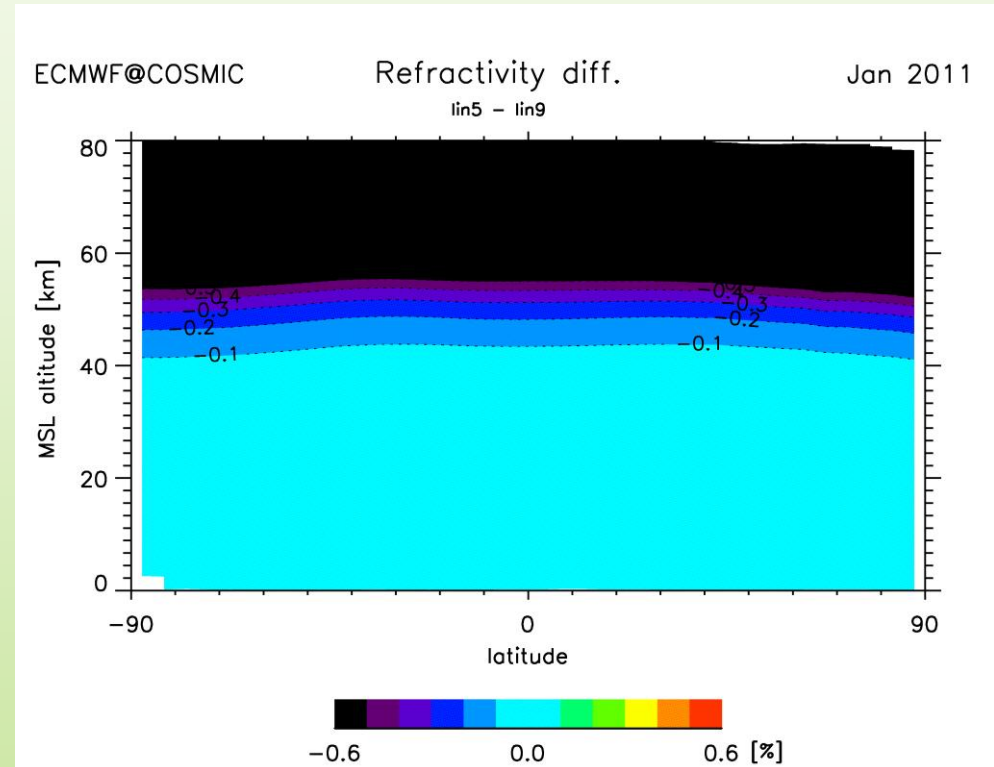
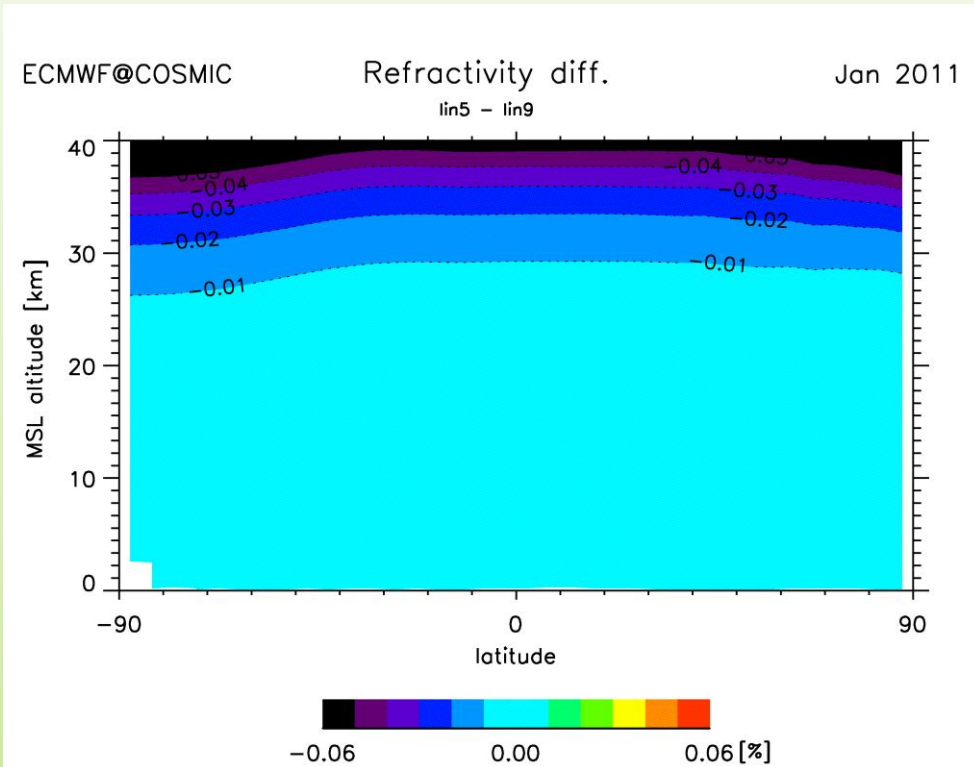
- differences between 5 and 9 km scale height –



**The impact of the extrapolation above 80 km is less than 0.01% at 25 km, and less than 0.1% at 40 km.**

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# BA to REF processing

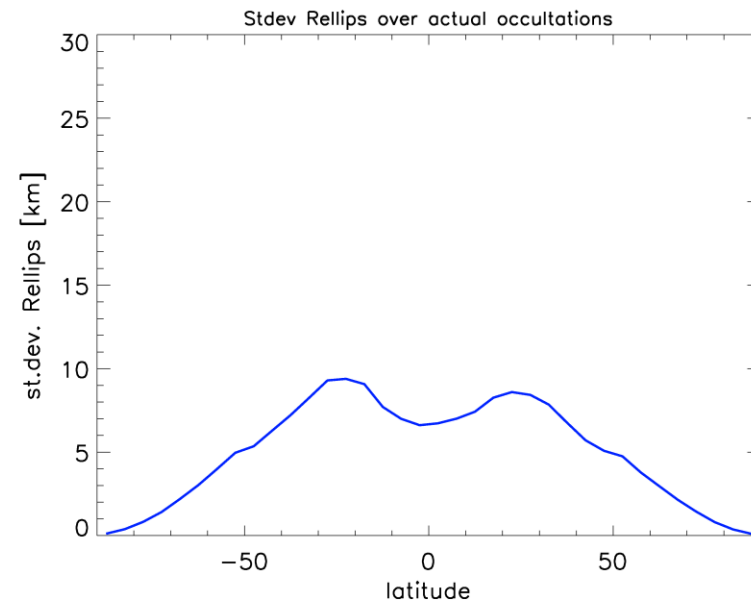
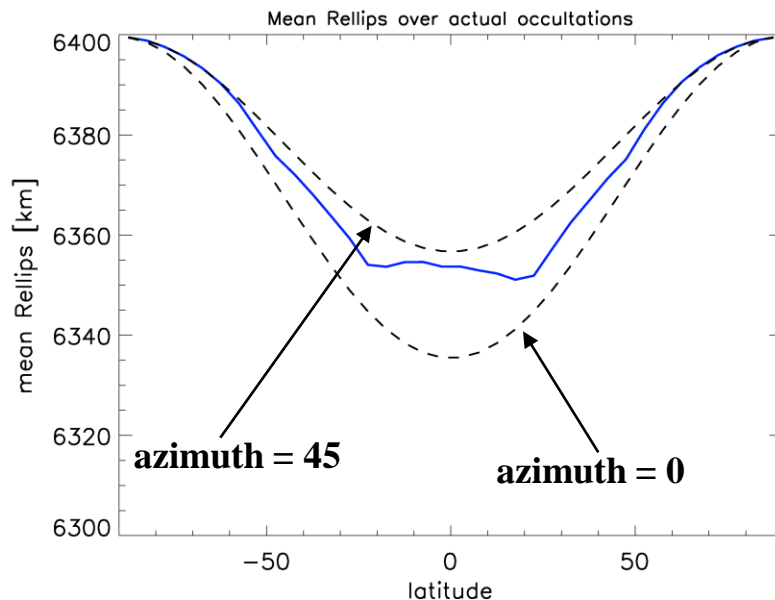
– zonal monthly means –

## Step 3: change of height scale (radius of curvature for grid boxes)

The mean field  $\langle \alpha(H_a) \rangle$  should be converted to  $\langle \alpha(a) \rangle$  before Abel.

Assign a single radius of curvature,  $R$ , to each grid box.

Each profile within a grid box has its own radius of curvature  $R + \Delta_i$ .



# BA to REF processing

– zonal monthly means –

Assume  $R = \bar{R} = \langle R_{c,i} + u_i \rangle$

If all profiles in the grid box had the same radius of curvature, the BAs at *impact altitude*  $H_a$  would be identical to the BAs at *impact parameter*  $a = H_a + R$ .

But the spread in *impact parameters*  $H_a + \bar{R} + \Delta_i$ , in combination with a non-linear  $\alpha(a)$  relation, leads to a bias in the mean BA at a fixed  $H_a + R$ .

$$\langle \alpha_i(H_a) \rangle \not\approx \langle \alpha_i(H_a + \bar{R}) \rangle$$

$$\langle \alpha_i(H_a) \rangle \Leftrightarrow \langle \alpha_i(H_a + \bar{R} + \Delta_i) \rangle = \langle \alpha_i(H_a + \bar{R}) \rangle + \delta$$

$$\delta \approx \frac{1}{2} \frac{d^2 \alpha}{da^2} \langle \Delta_i^2 \rangle$$

# BA to REF processing

– zonal monthly means –

This bias can be partly offset by assuming that  $R = \bar{R} + \Delta R$ , where  $\Delta R$  is chosen such that

$$\frac{d\alpha}{da} \Delta R + \delta = 0$$

## Step 4: inverse Abel transform

$$\langle N(x) \rangle = 10^6 \exp \left( \frac{1}{\pi} \int_x^\infty \frac{\langle \alpha(a) \rangle}{(a^2 - x^2)^{1/2}} da \right) - 10^6$$

## Step 5: change of height scale

$$\langle N(a) \rangle \mapsto \langle N(H) \rangle = \langle N(a / (1 + 10^{-6} N(a)) - R) \rangle$$

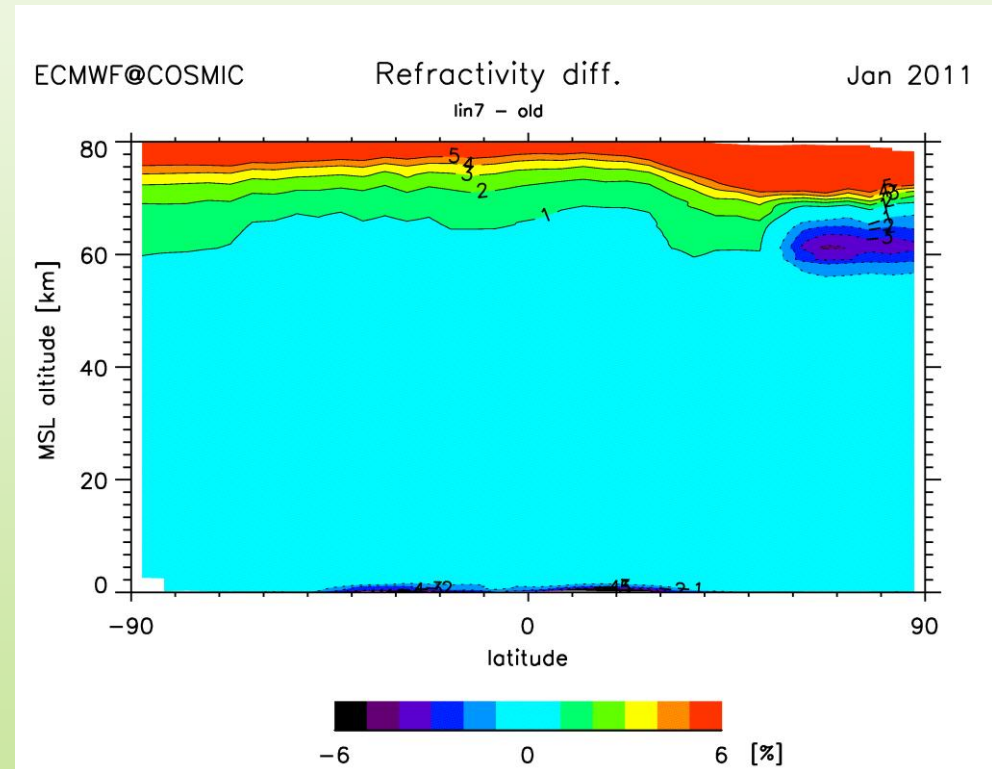
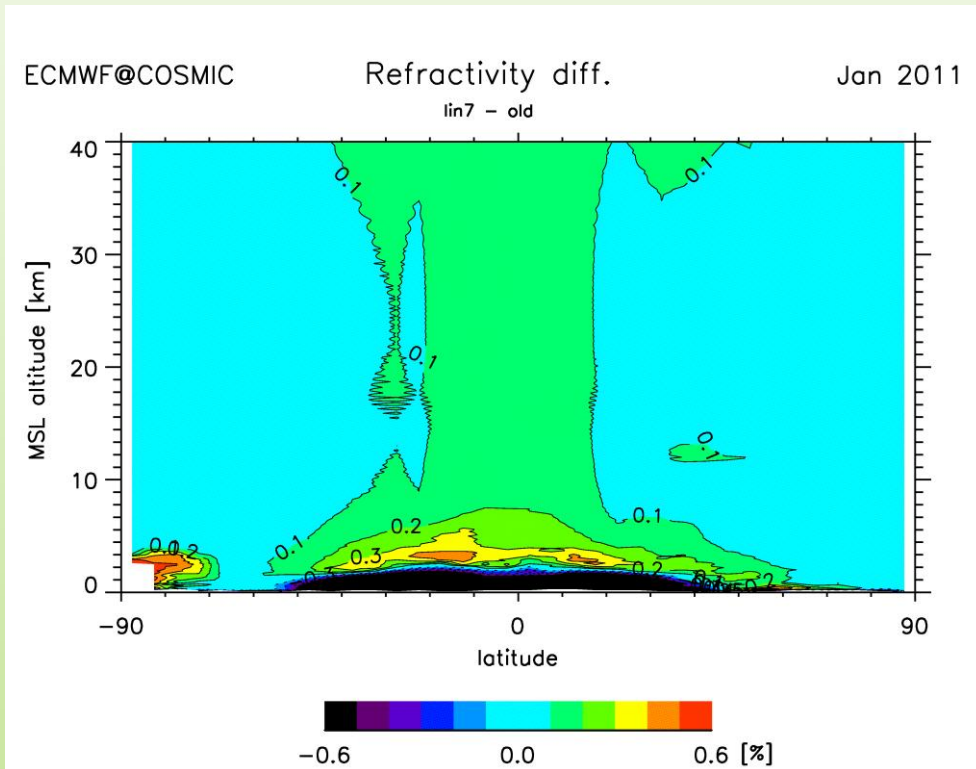


# Mean-field versus single-profile processing

– relative differences (collocated ECMWF) –

$H < 60$  km: mean;  $H = 60$ -80 km: median;  $H > 80$  km: exponential with 7.5 km scale height

**R:** radius of curvature for  $a_z = 0$

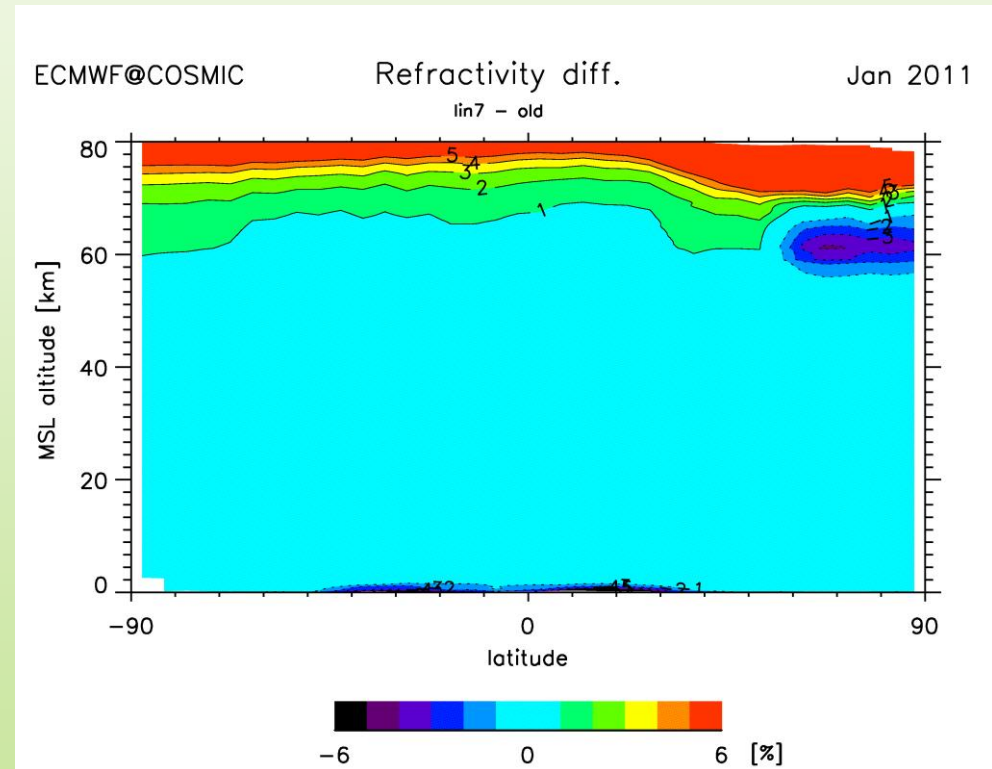
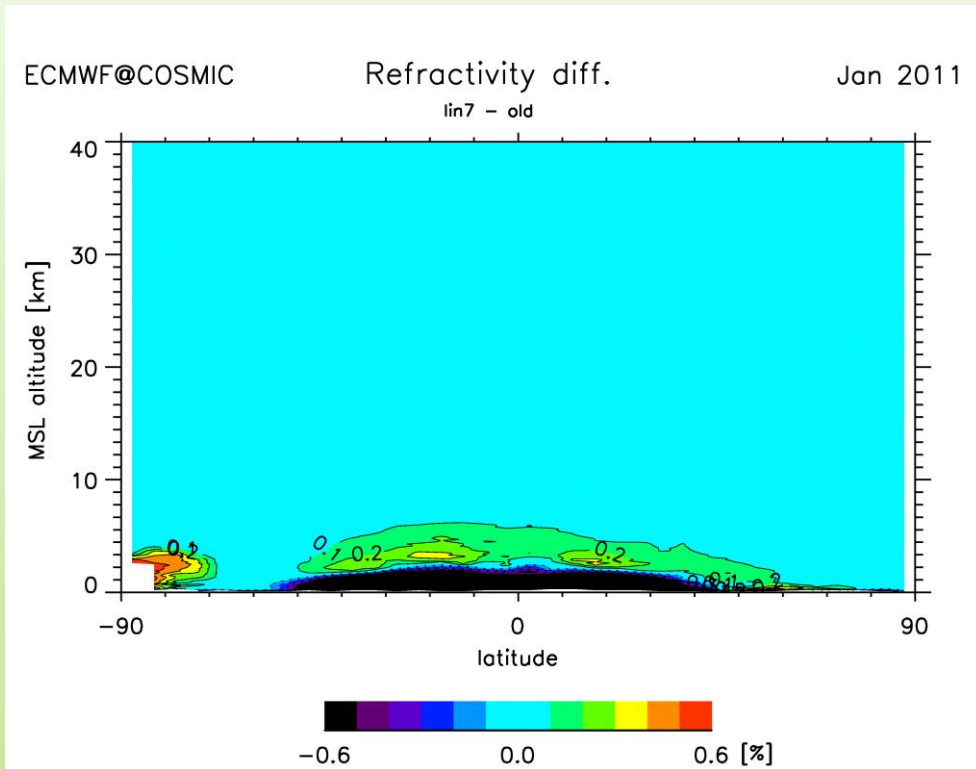


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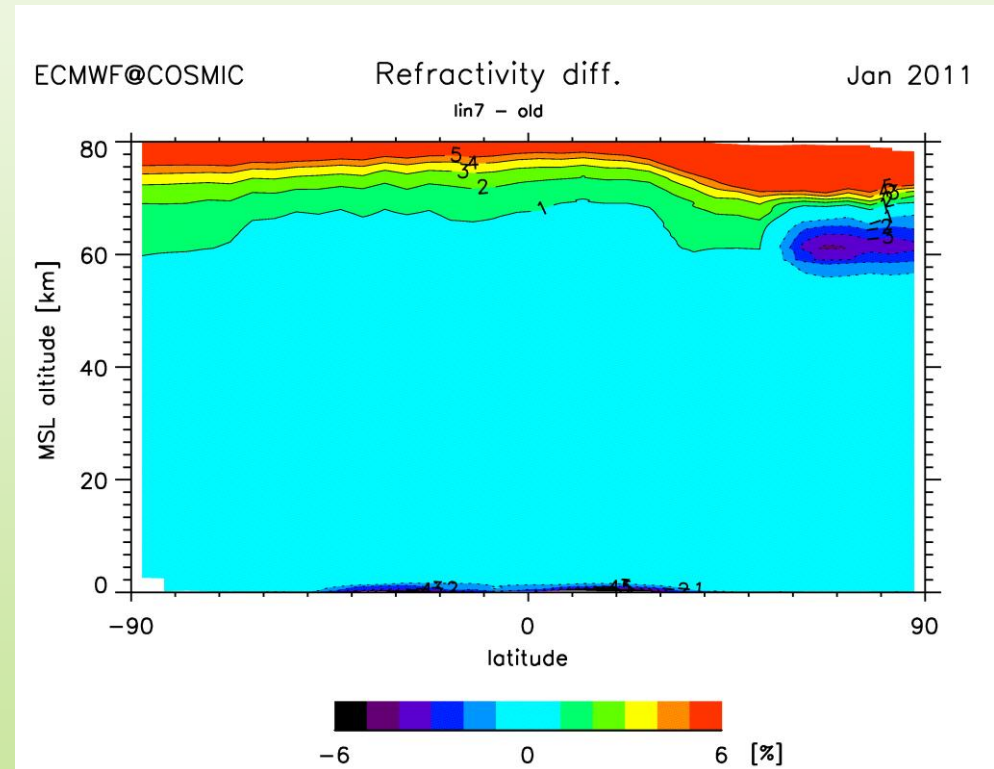
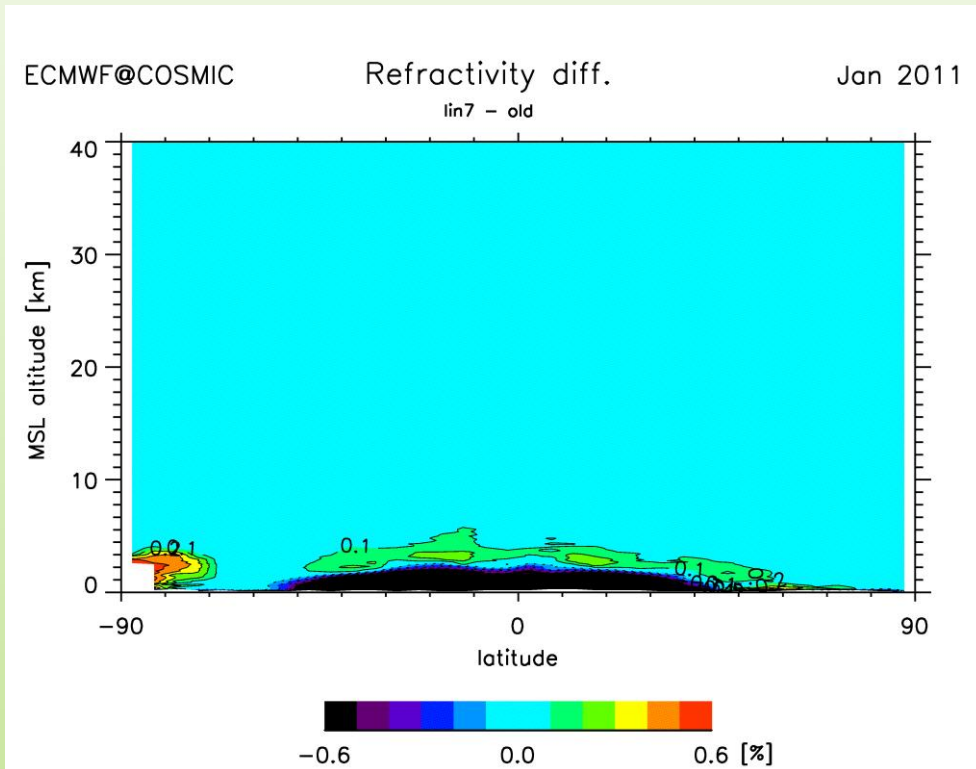


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– relative differences (collocated ECMWF) –

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**R:** mean radius of curvature + simple correction

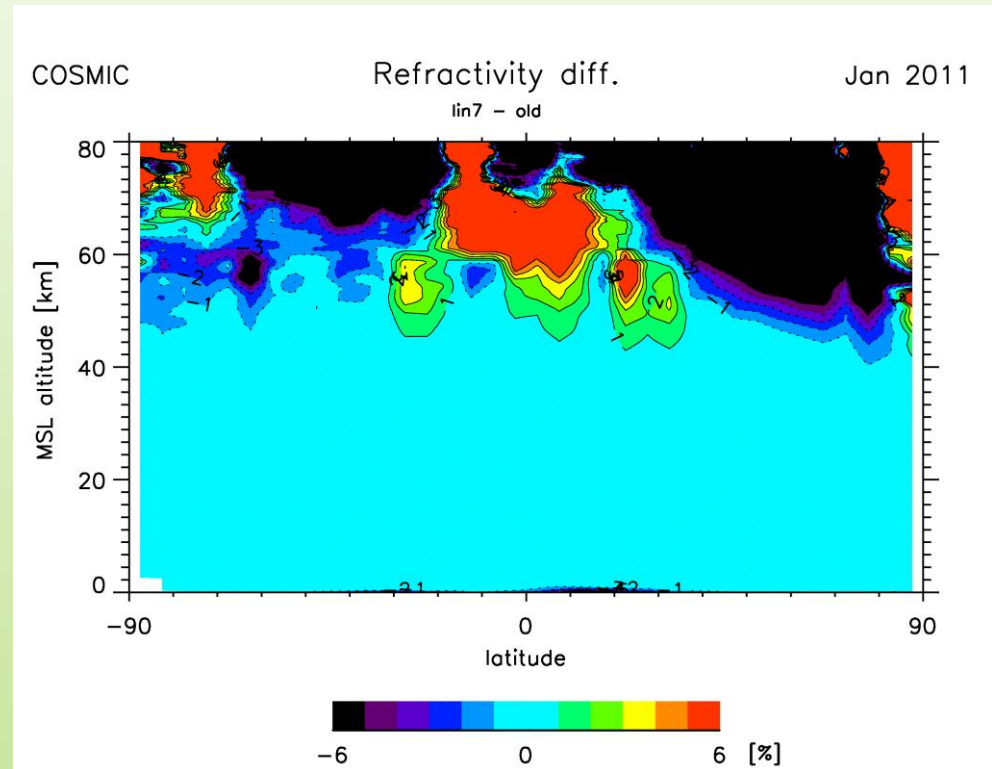
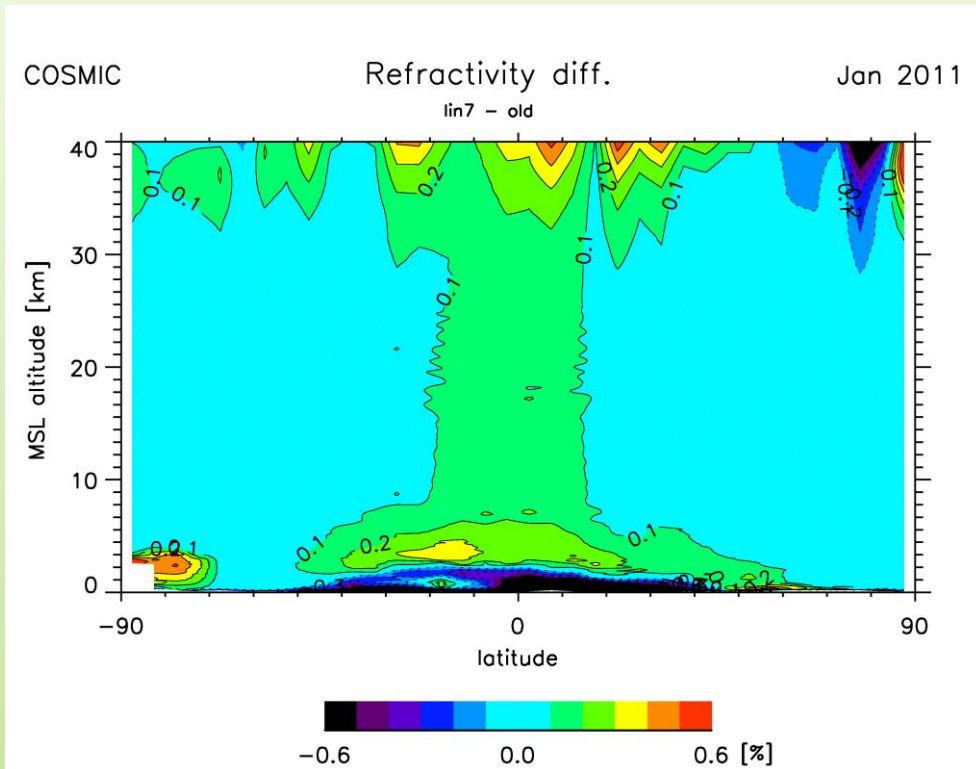


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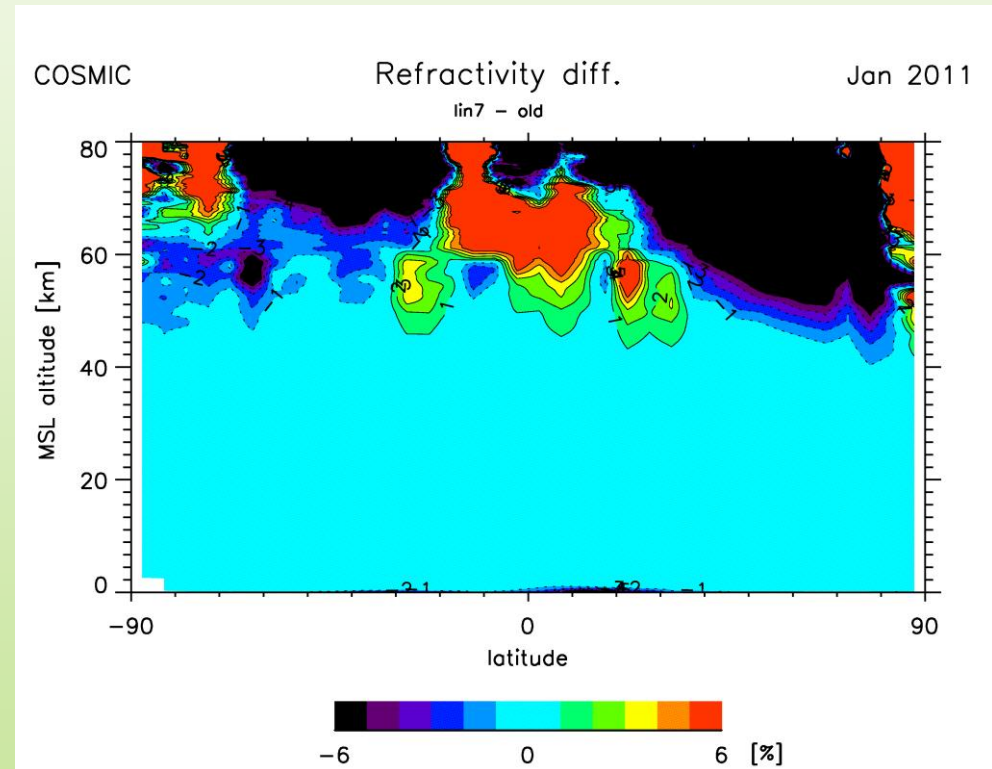
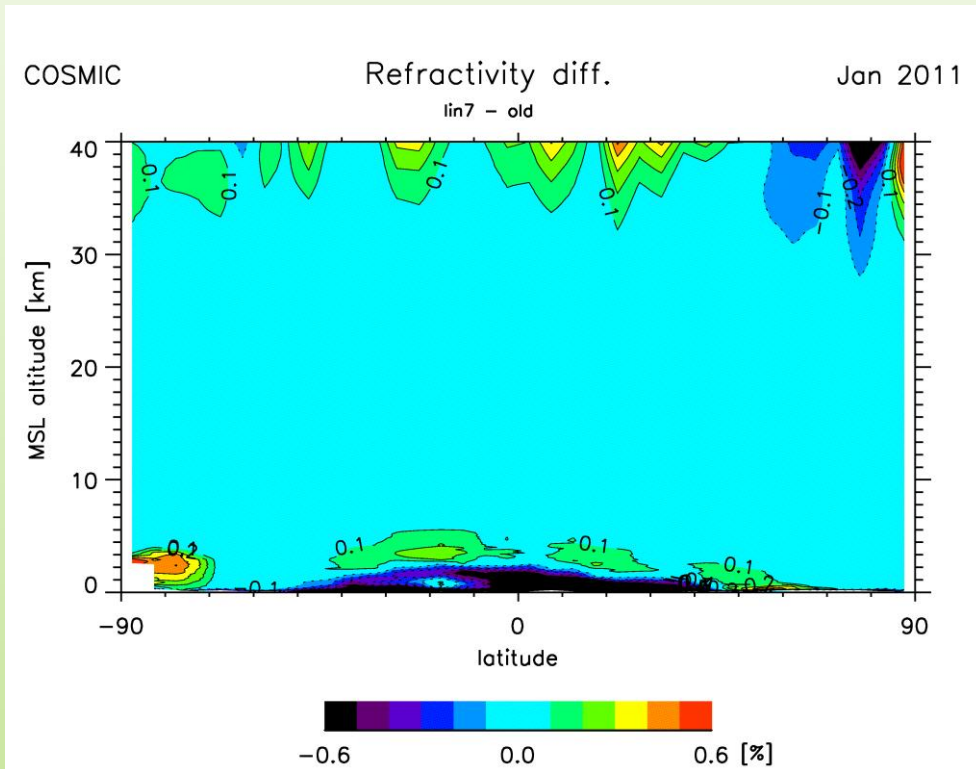


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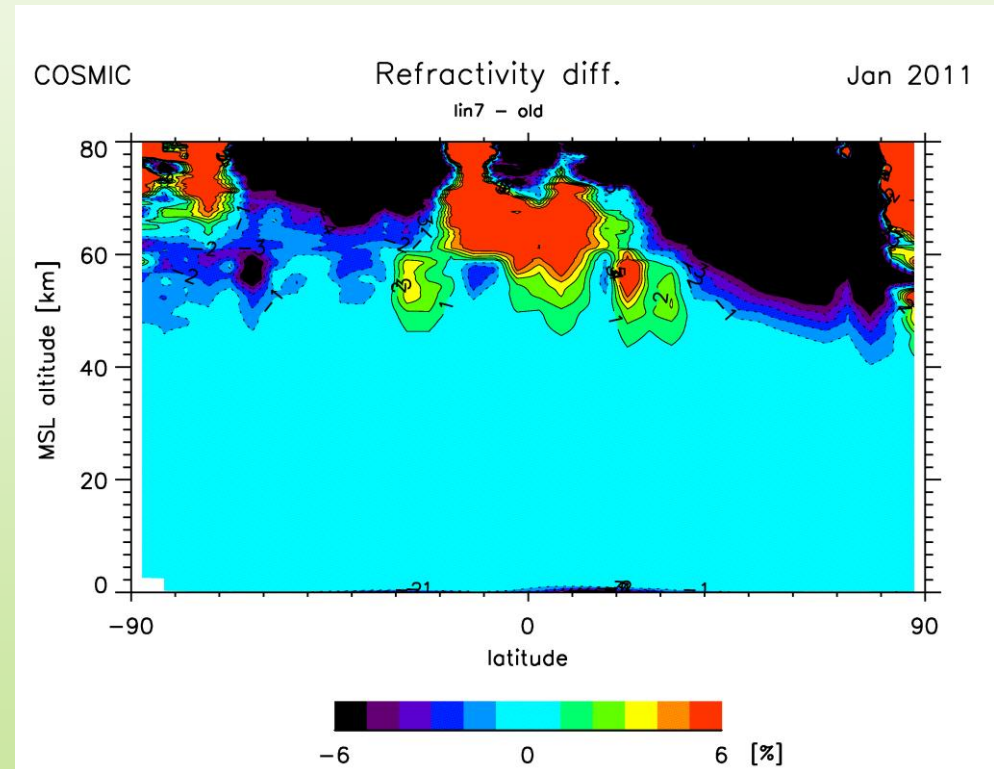
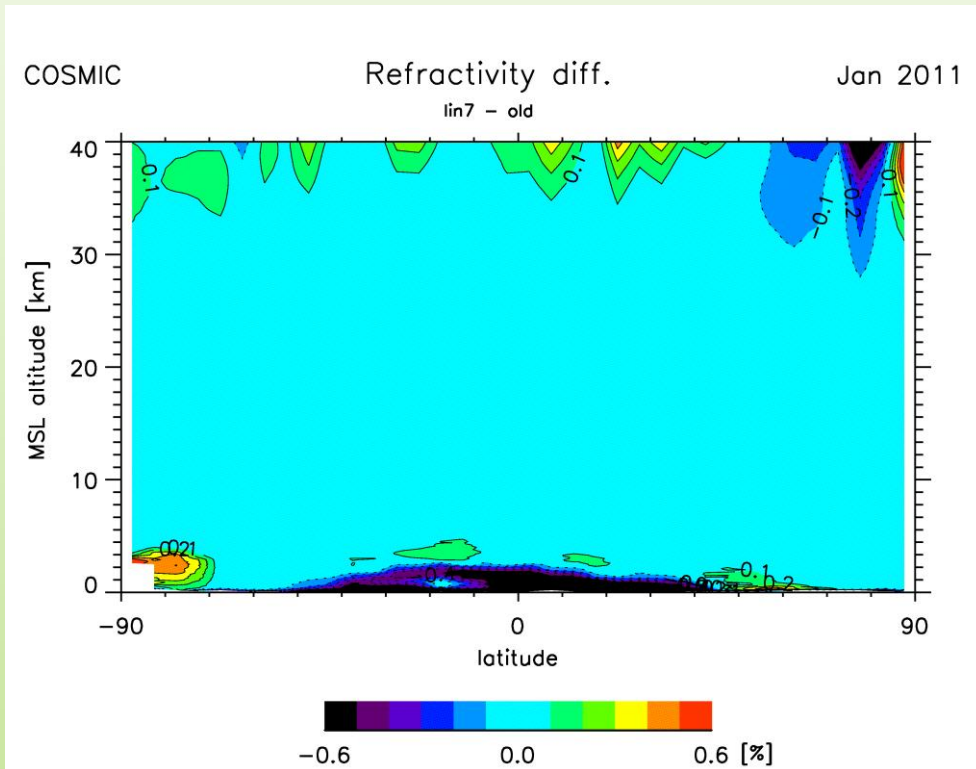


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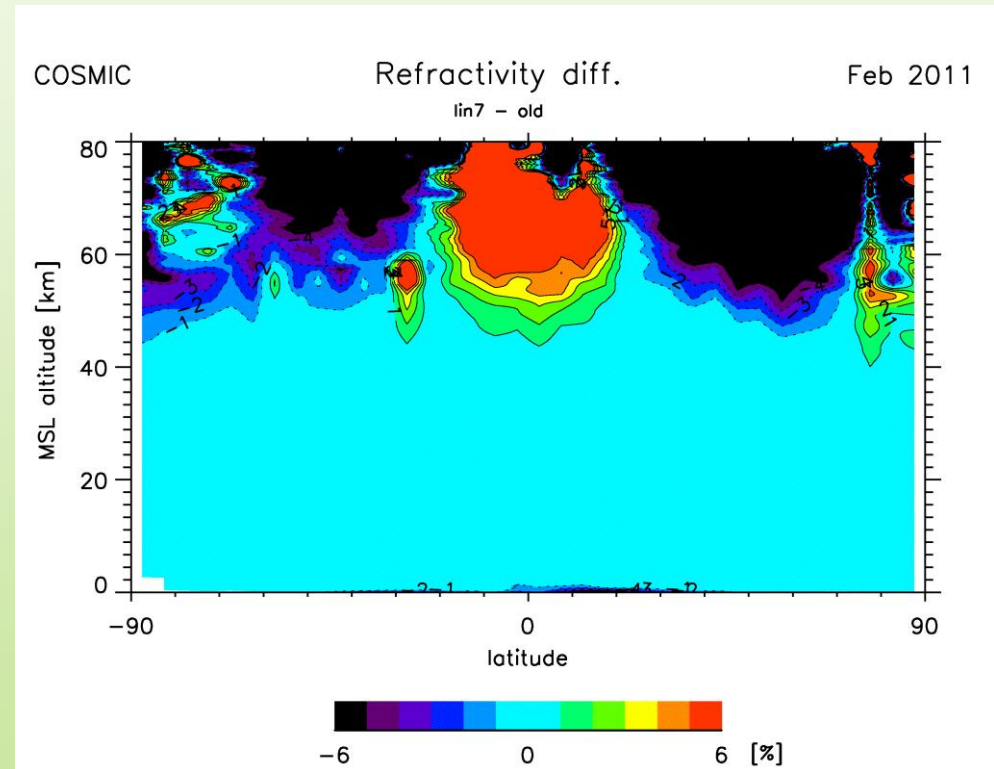
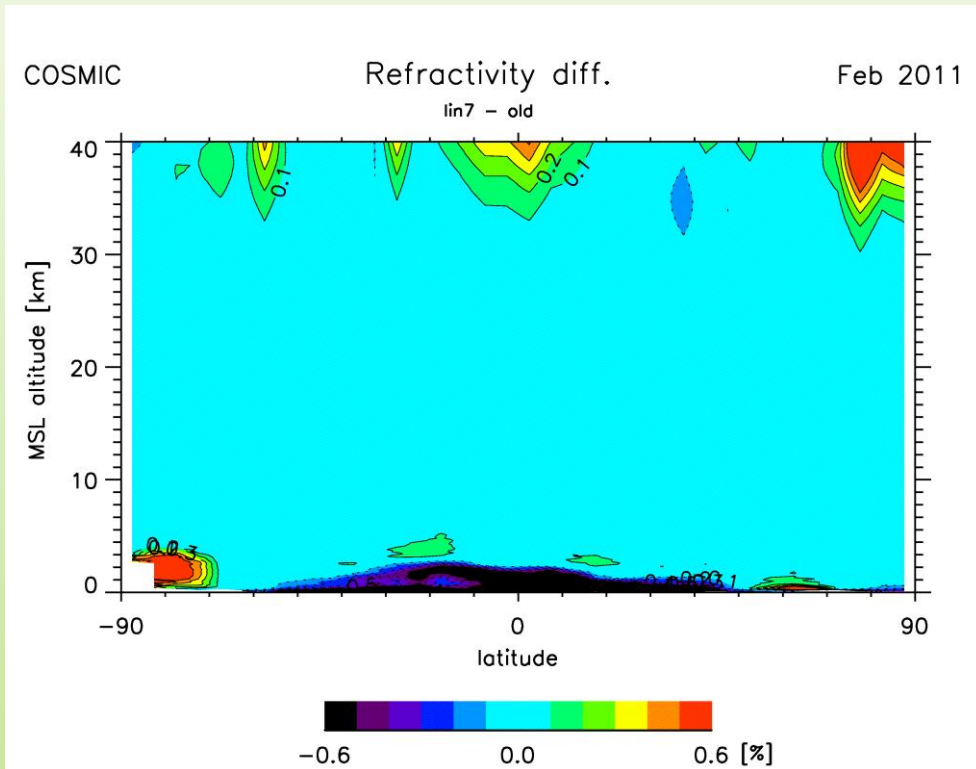


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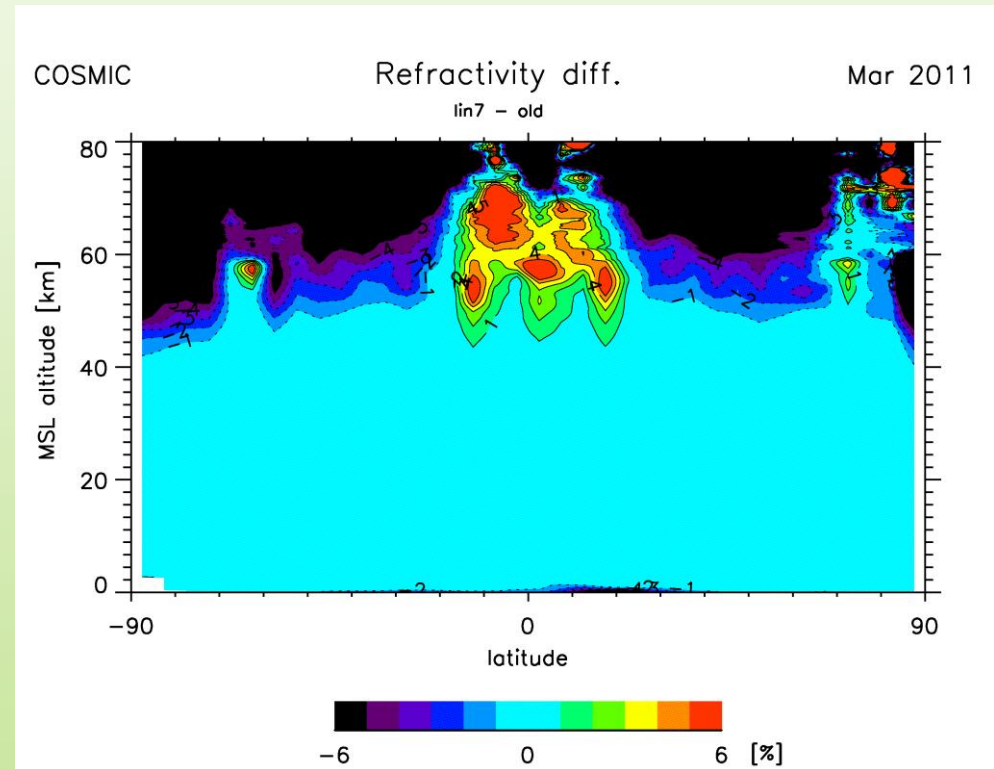
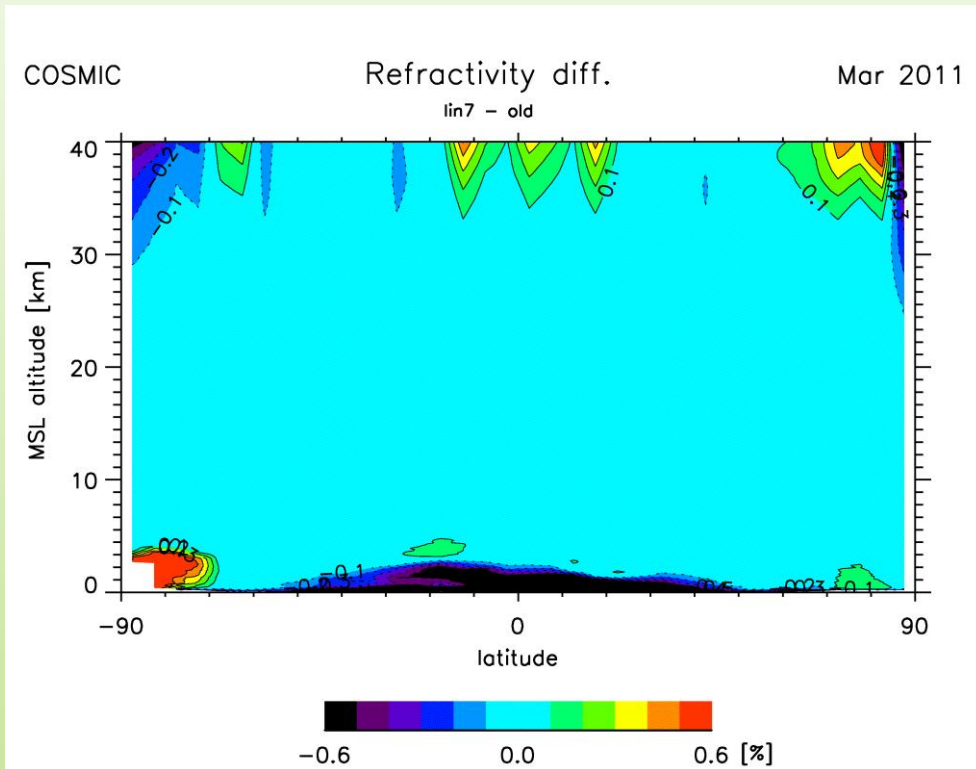


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# Conclusions

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- ▶ mean-field processing is an option when there are many enough profiles in each grid box – we can do without stat. opt.
- ▶ above 60 km the means become noisy – medians can still be used
- ▶ above 80 km exponential extrapolation is sufficient
- ▶ less than 0.1% difference from single-profile processing above lower troposphere, up to 1.0% difference in the lowest few kilometers
- ▶ profile-to-profile variability in radius of curvature within grid boxes needs to be handled – corrections can be devised

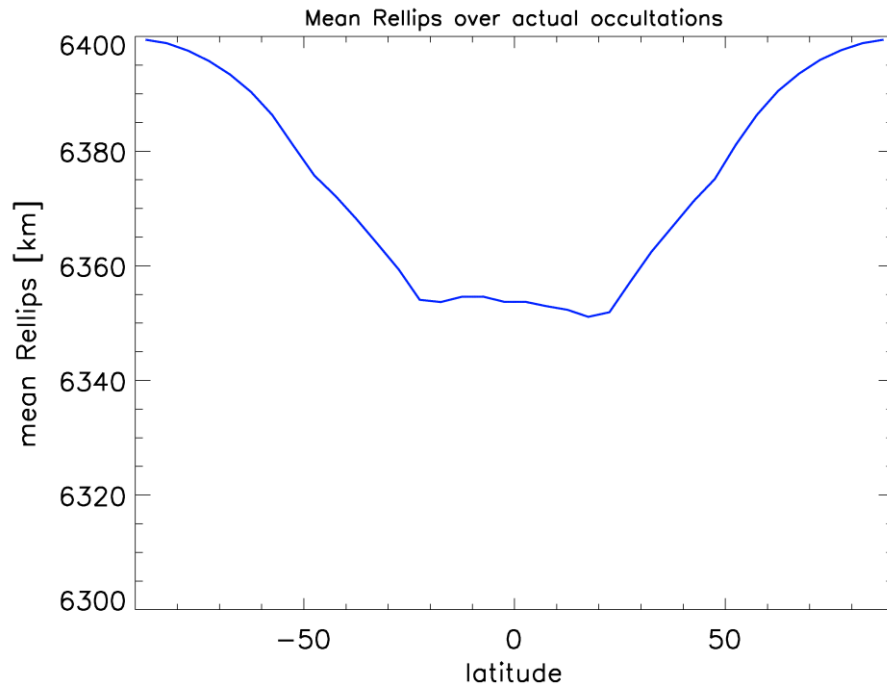
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# STOP

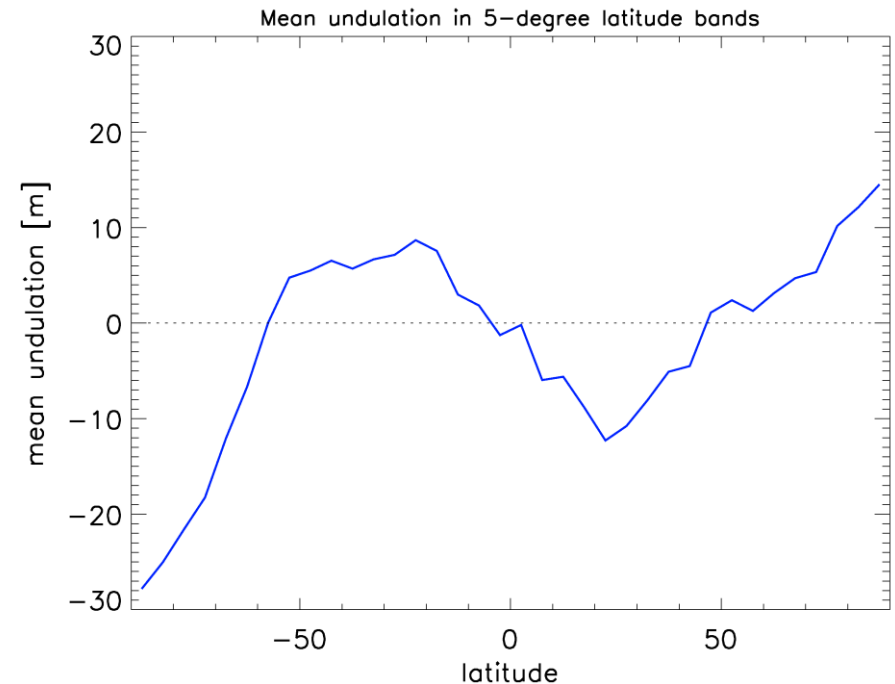
# *BA to REF processing*

- radius of curvature variability –

## Mean radius of curvature



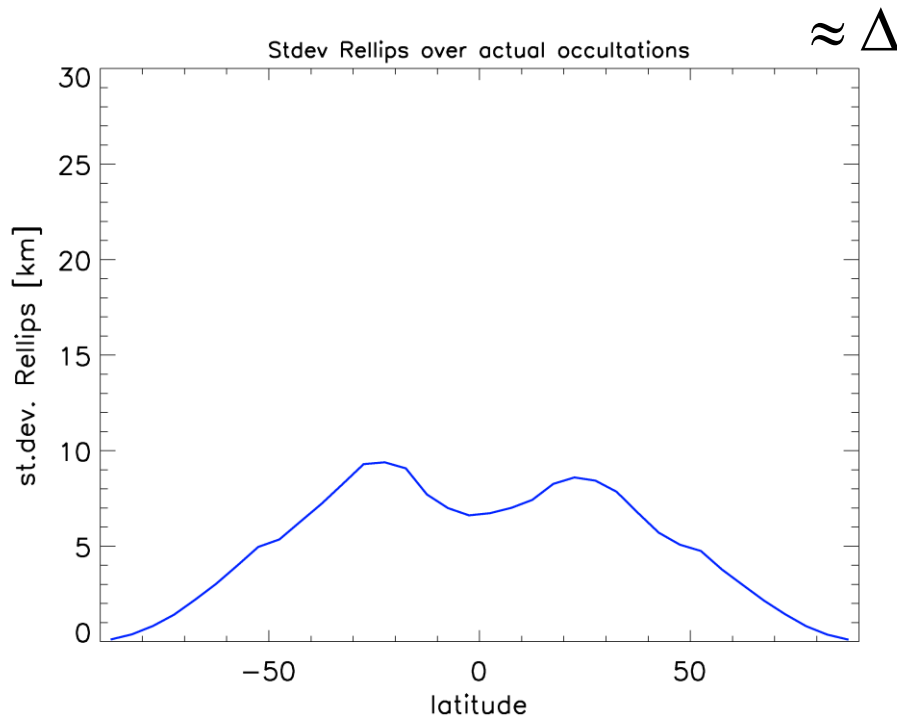
## Mean undulation



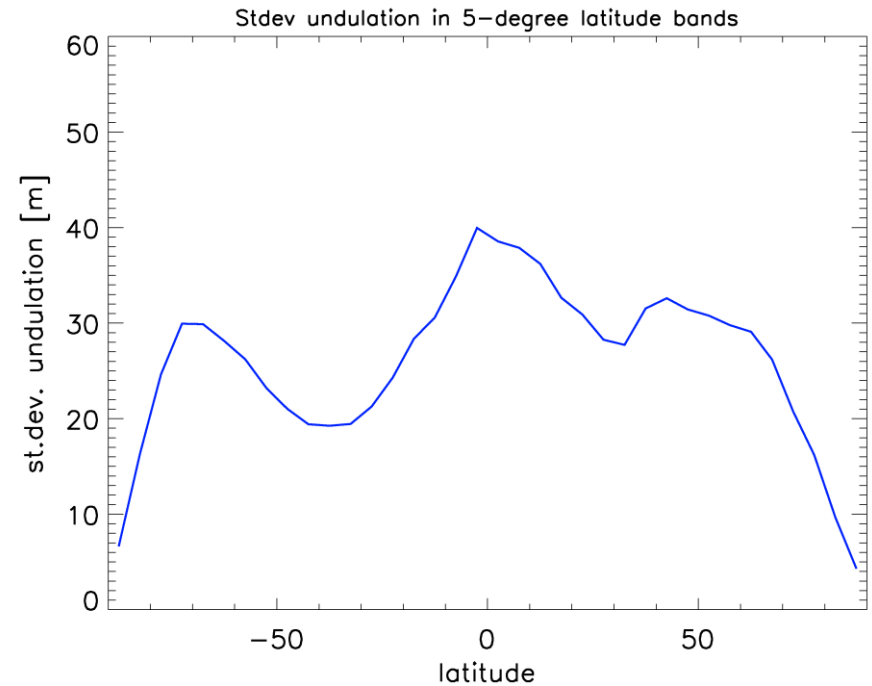
# *BA to REF processing*

- radius of curvature variability –

## St.dev radius of curvature

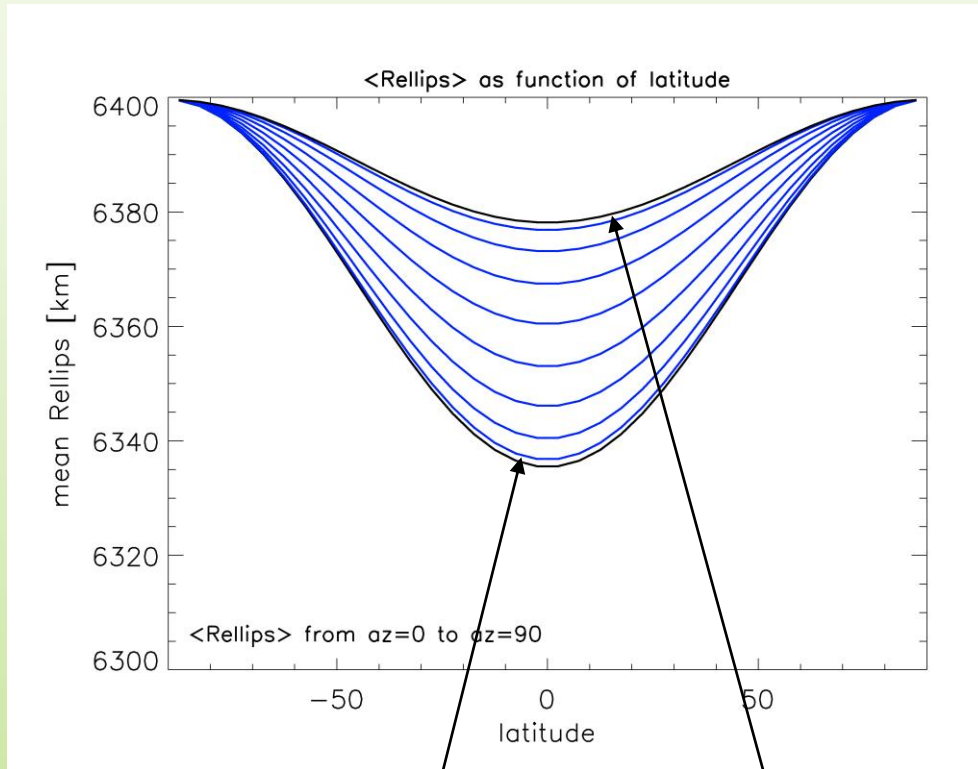


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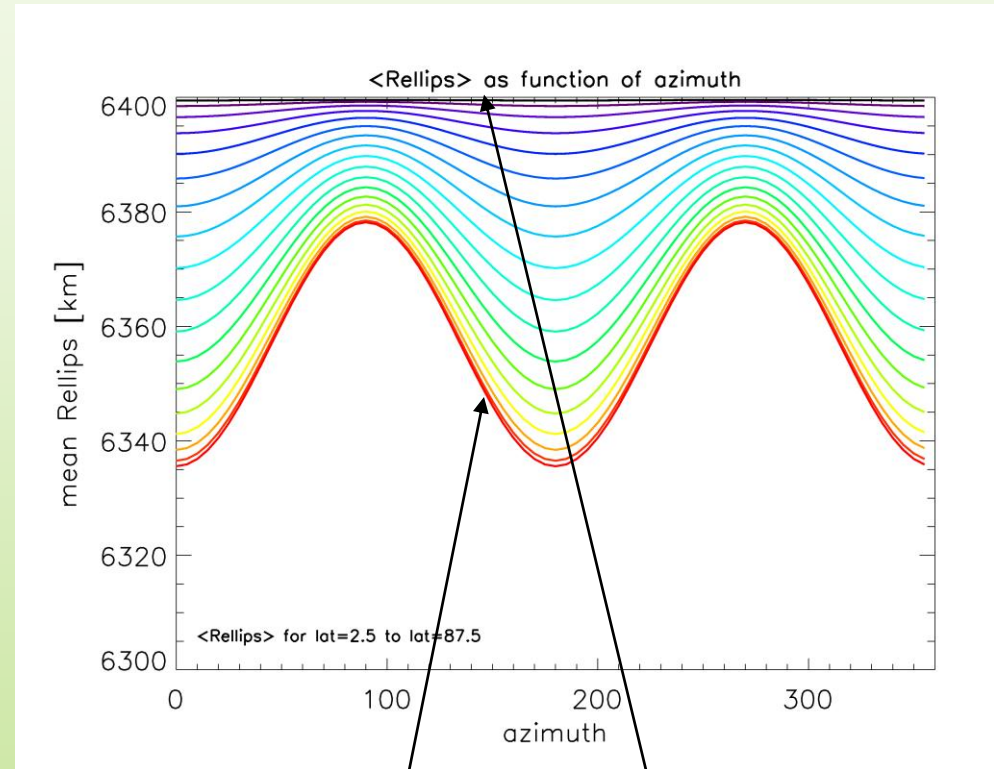
# Ellipsoid radius of curvature

– longitudinal averages –



**azimuth = 0**

**azimuth = 90**

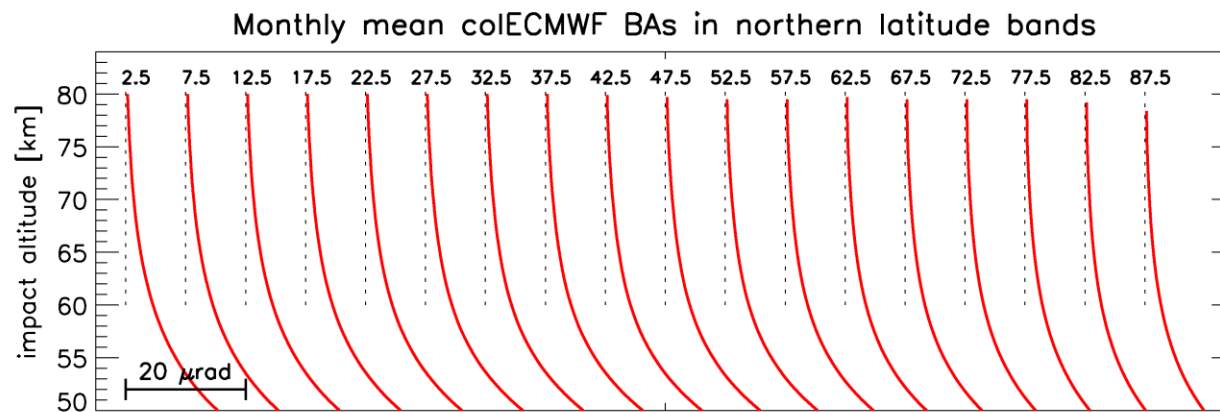
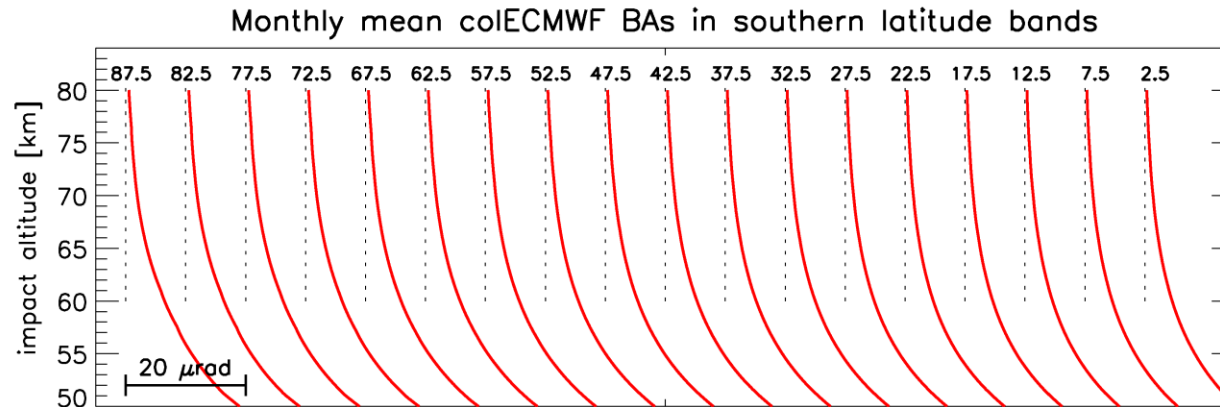


**latitude = 2.5**

**latitude = 87.5**

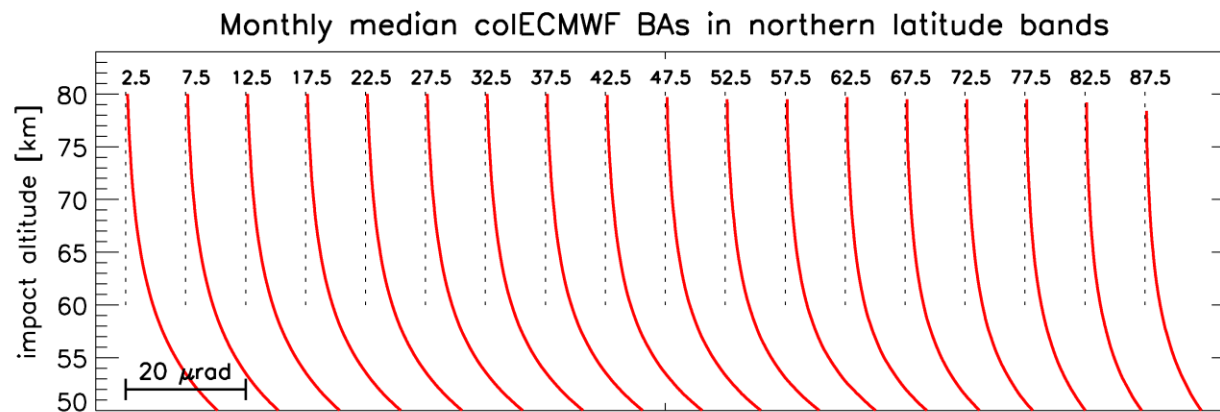
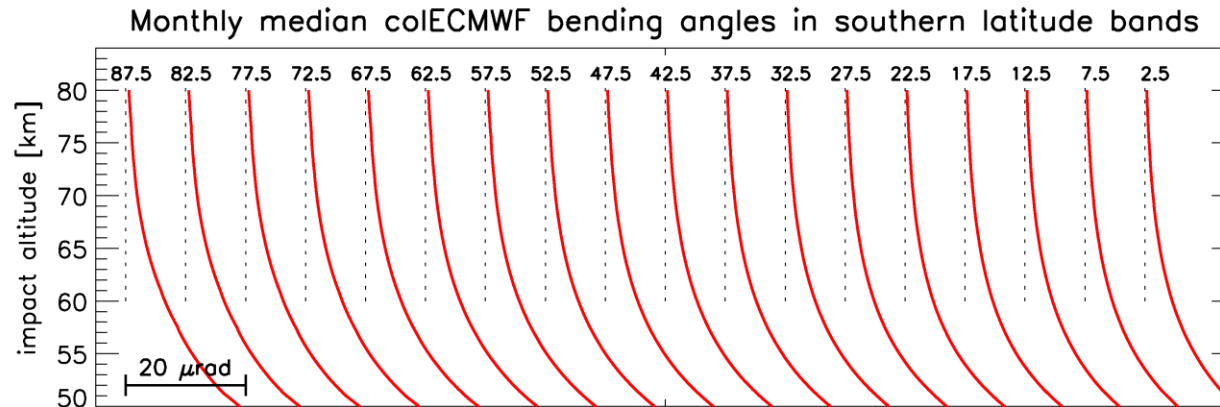
# Monthly mean bending angles

– means, ECMWF (colloc.), Jan 2011 –



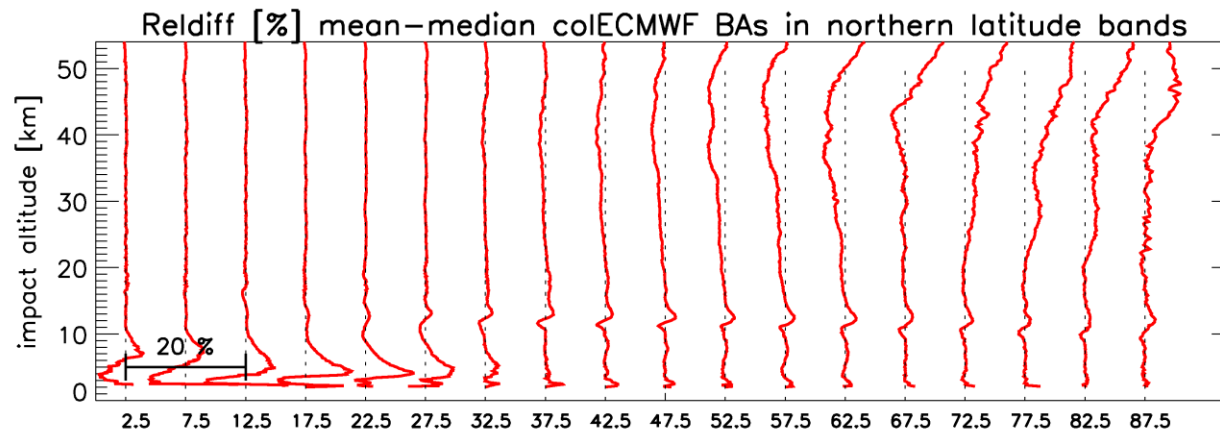
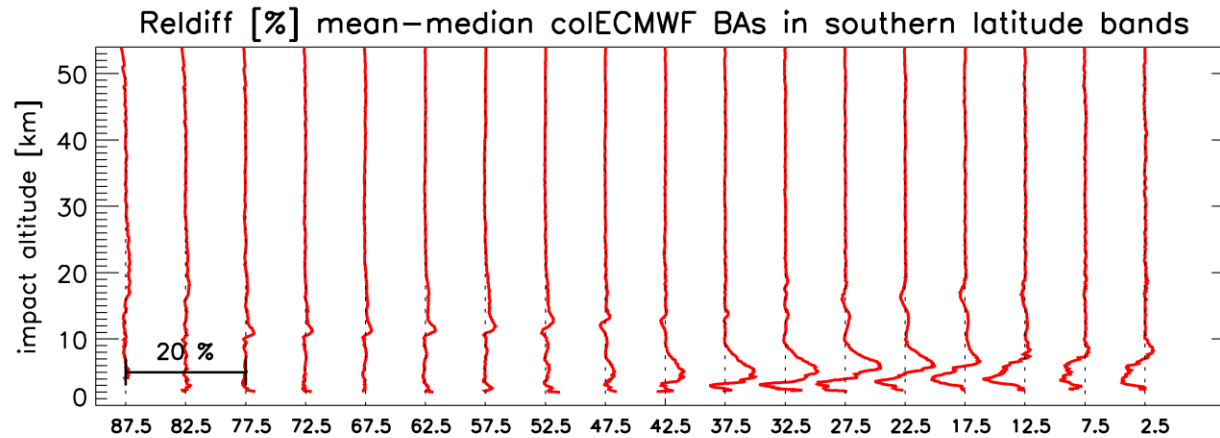
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